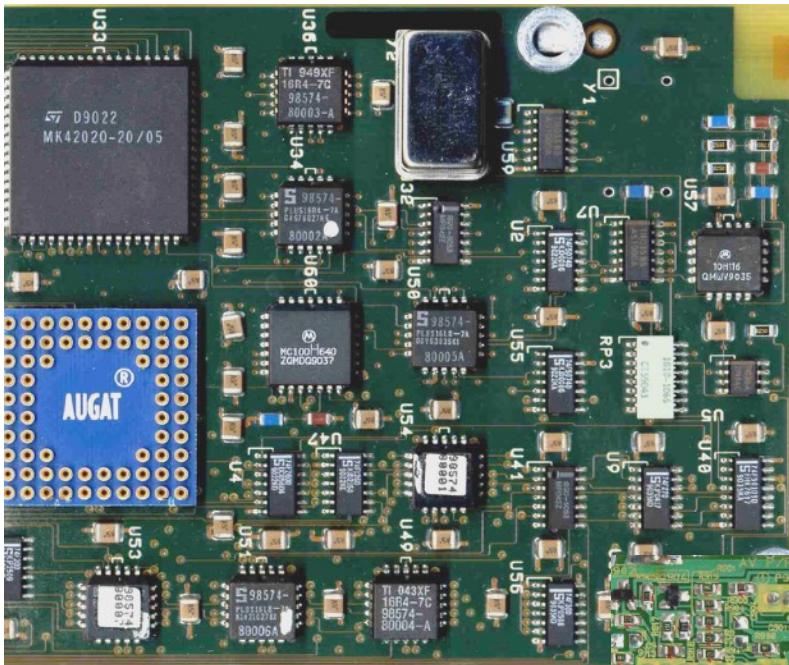


Circuits II - circuits électroniques et filtrage

EPFL

D. Mari

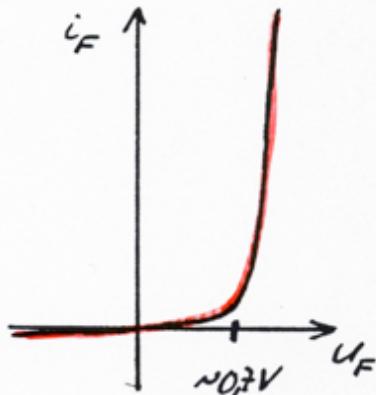
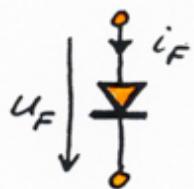


Circuits électroniques

On appellera circuits électroniques des circuits électriques dans lesquels interviennent **des éléments non-linéaires et/ou des éléments actifs**.

Eléments non-linéaires

Diodes

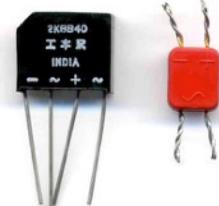


$$i = f_{ne}(u) \Rightarrow \text{résistance non linéaire}$$

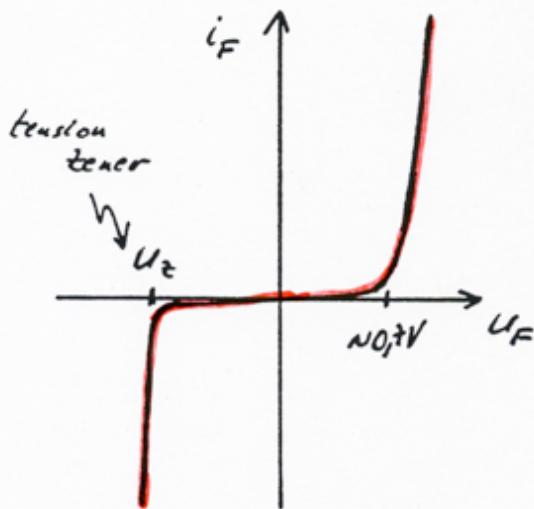
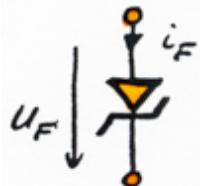
$$i_F = i_{so} \left[e^{\frac{eU_F}{kT}} - 1 \right]$$

i_{so} = courant inverse de saturation

e =charge de l'électron



Diodes Zener



$$i = f_{ne}(u)$$

\Rightarrow résistance non linéaire

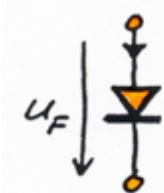
$$u_z \in [2V, 100V]$$

Circuits électroniques

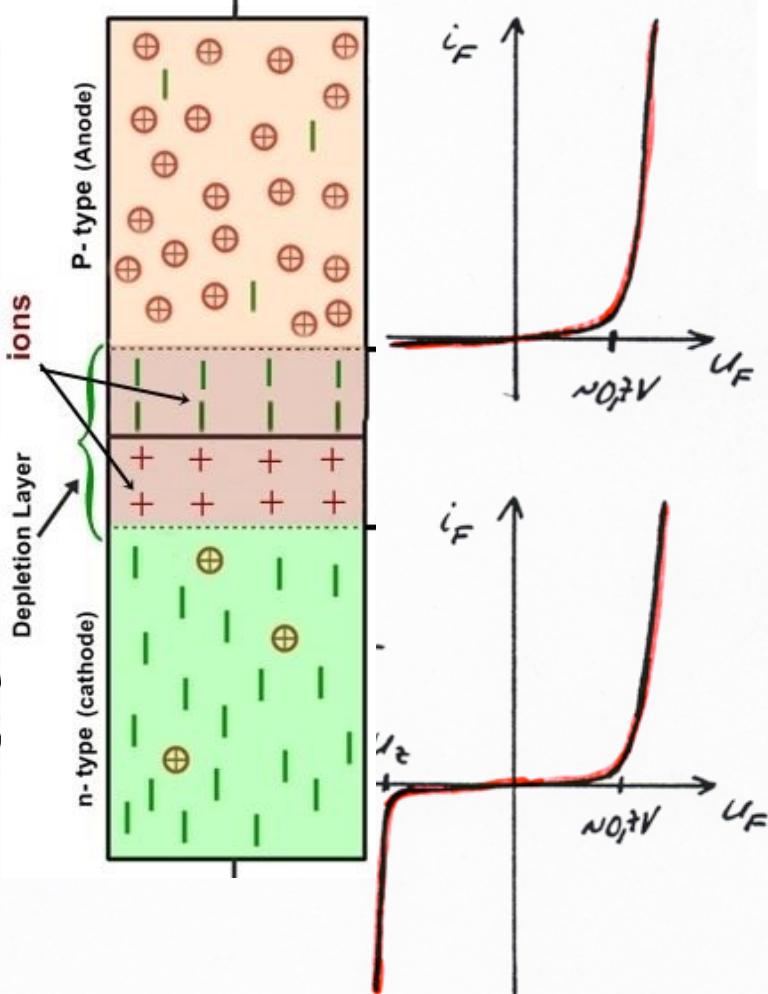
On appellera circuits électroniques des circuits électriques dans lesquels interviennent **des éléments non-linéaires et/ou des éléments actifs**.

Eléments non-linéaires

Diodes



Diodes

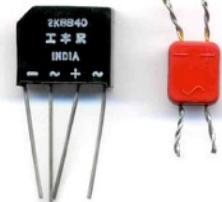


$$i = f_{ne}(u) \Rightarrow \text{résistance non linéaire}$$

$$i_F = i_{so} \left[e^{\frac{eU_F}{kT}} - 1 \right]$$

i_{so} = courant inverse de saturation

e =charge de l'électron



$$i = f_{ne}(u)$$

\Rightarrow résistance non linéaire

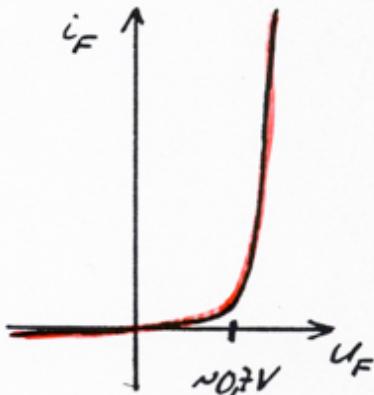
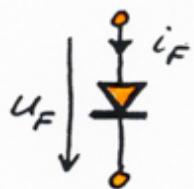
$$u_z \in [2V, 100V]$$

Circuits électroniques

On appellera circuits électroniques des circuits électriques dans lesquels interviennent **des éléments non-linéaires et/ou des éléments actifs**.

Eléments non-linéaires

Diodes

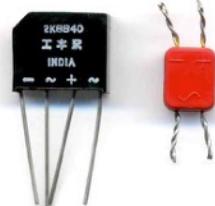


$$i = f_{ne}(u) \Rightarrow \text{résistance non linéaire}$$

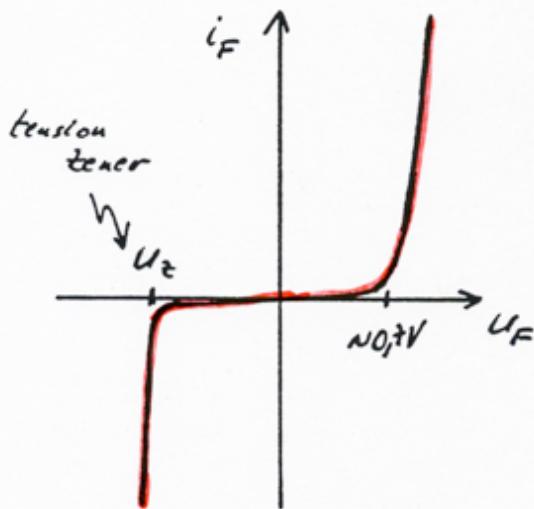
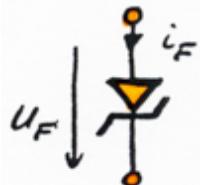
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i_{so} = courant inverse de saturation

e =charge de l'électron



Diodes Zener



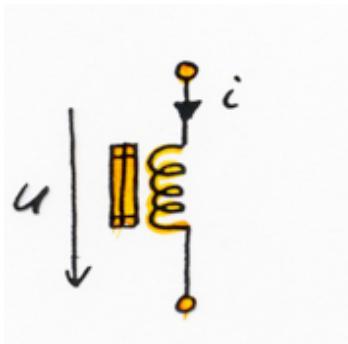
$$i = f_{ne}(u)$$

\Rightarrow résistance non linéaire

$$u_z \in [2V, 100V]$$

Eléments non-linéaires

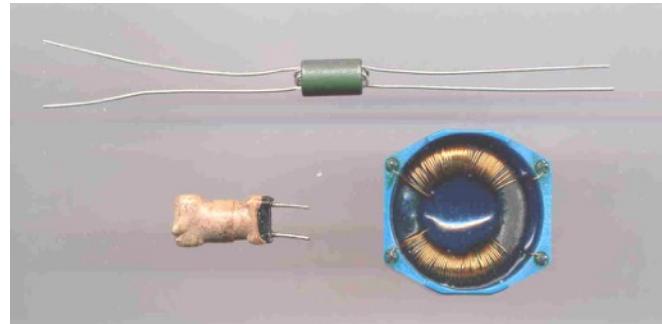
Selfs à noyau magnétique



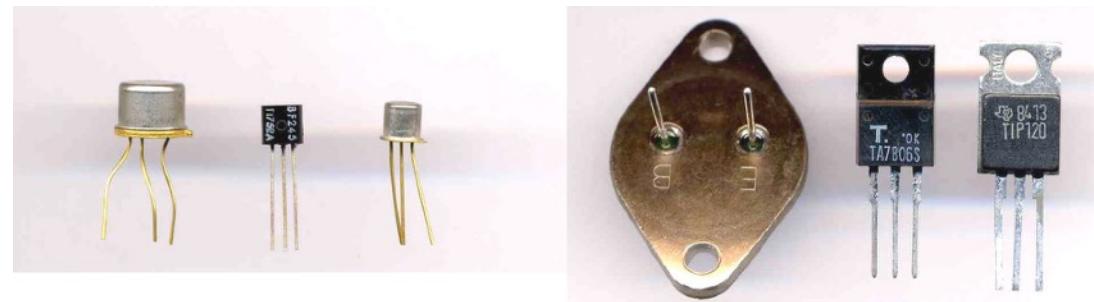
$$\phi = f_{nl}(i)$$

$$u = \frac{d\phi}{dt}$$

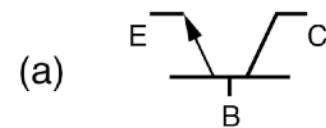
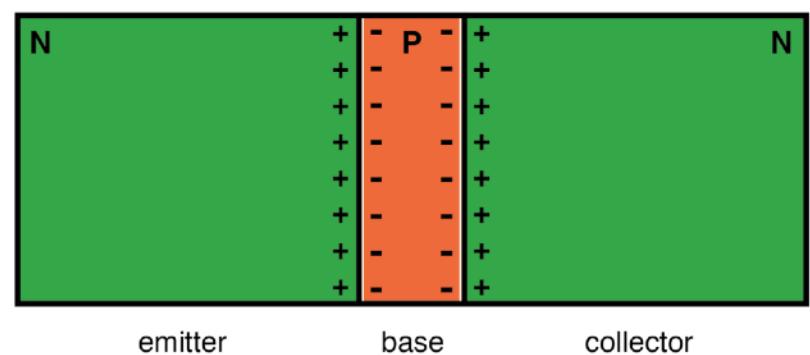
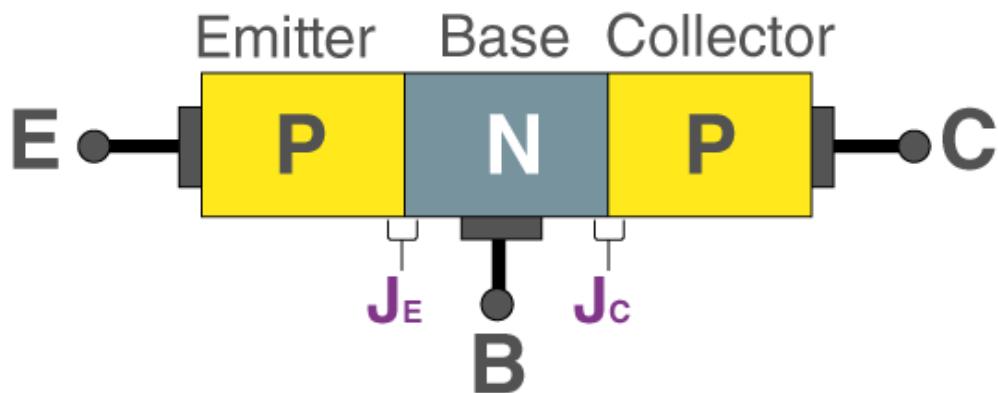
\Rightarrow inductance non linéaire



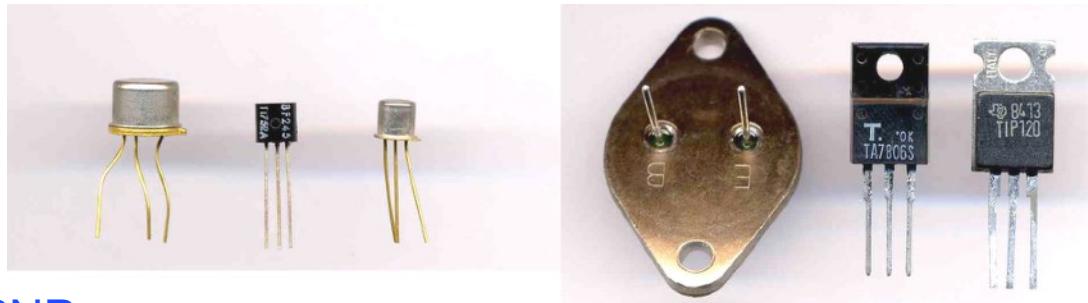
Eléments actifs



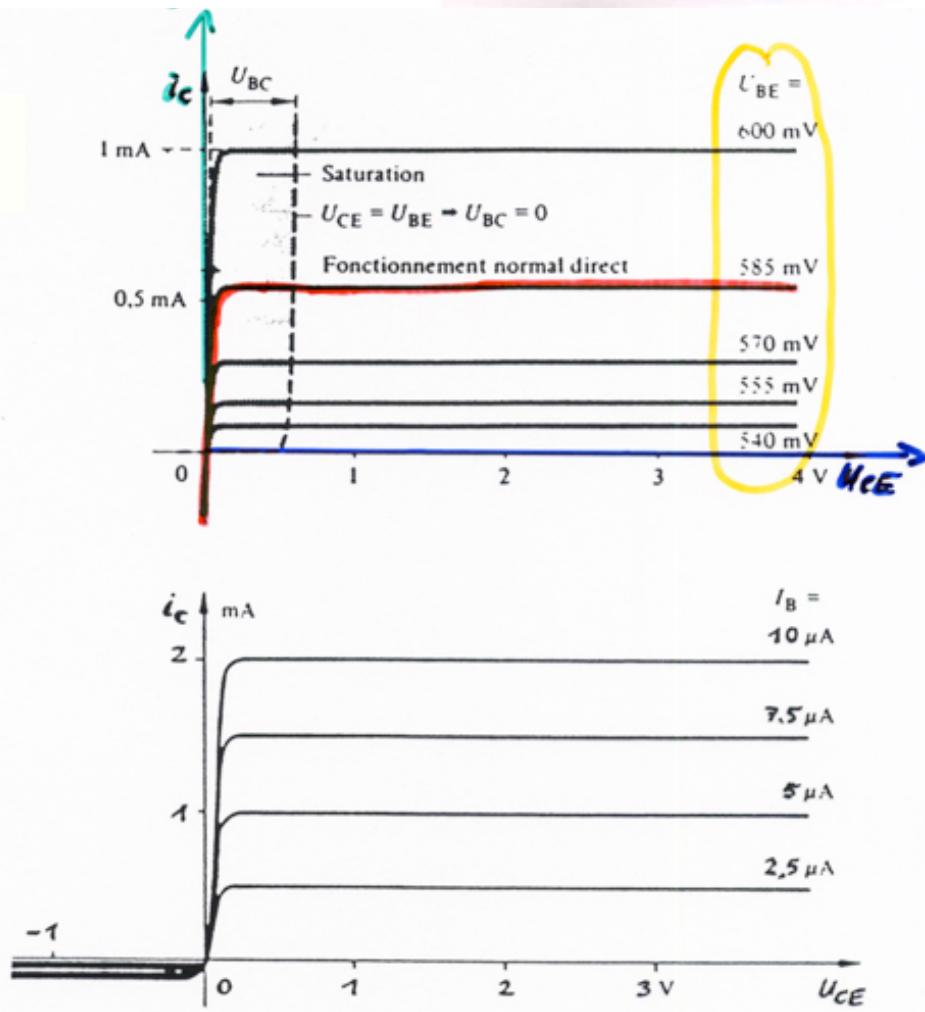
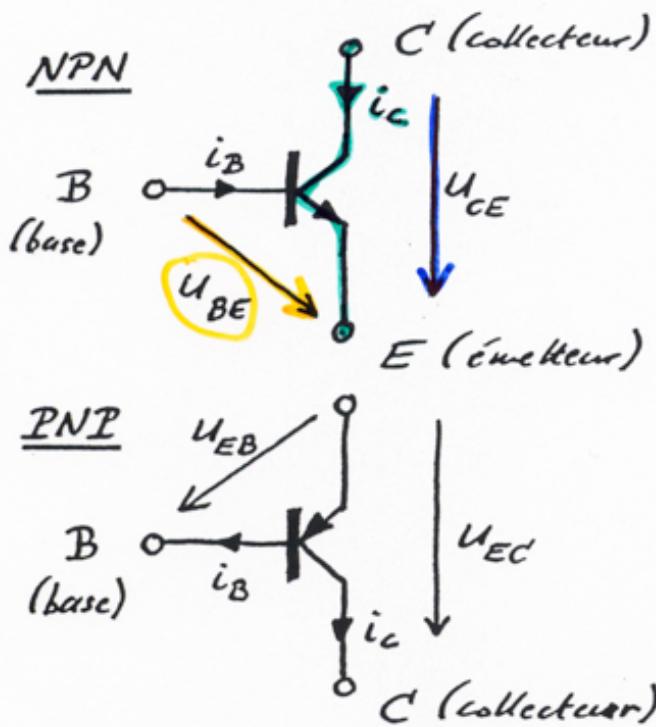
Transistors bipolaires PNP et NPN



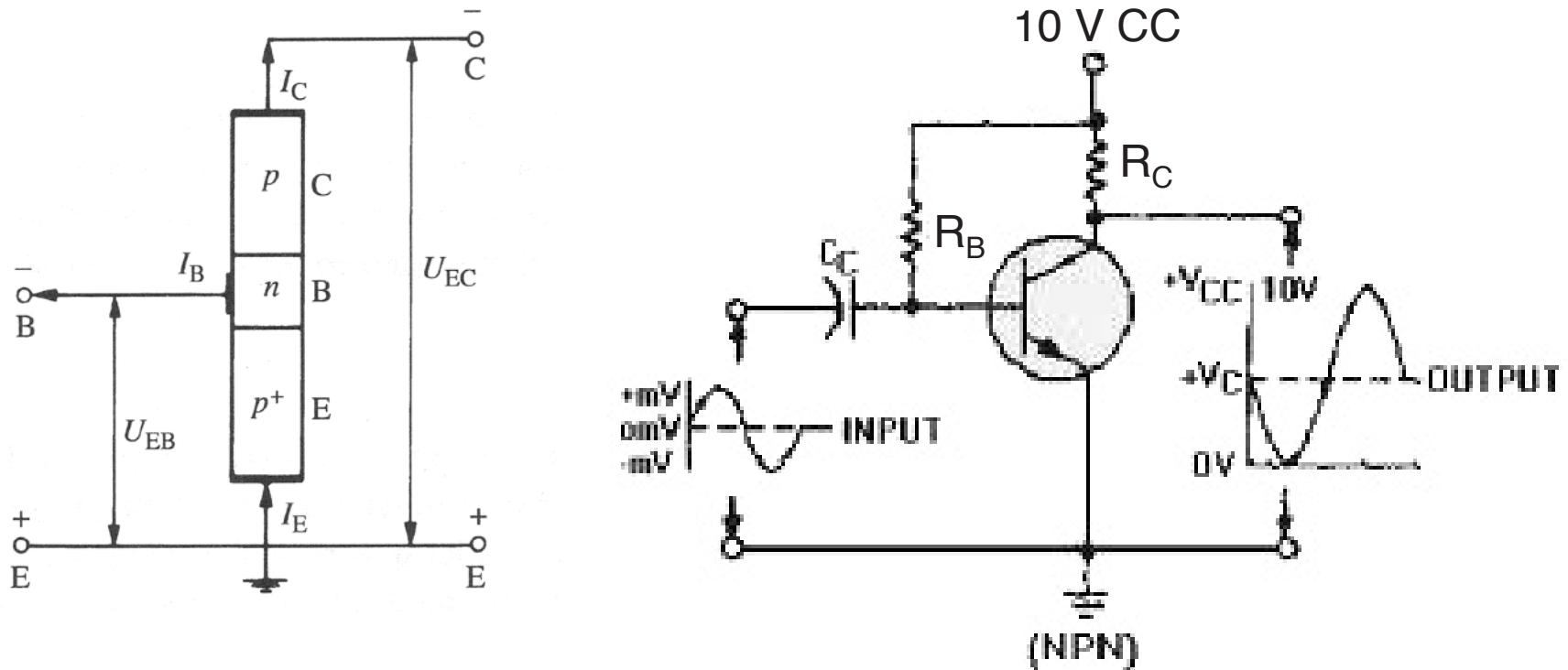
Eléments actifs



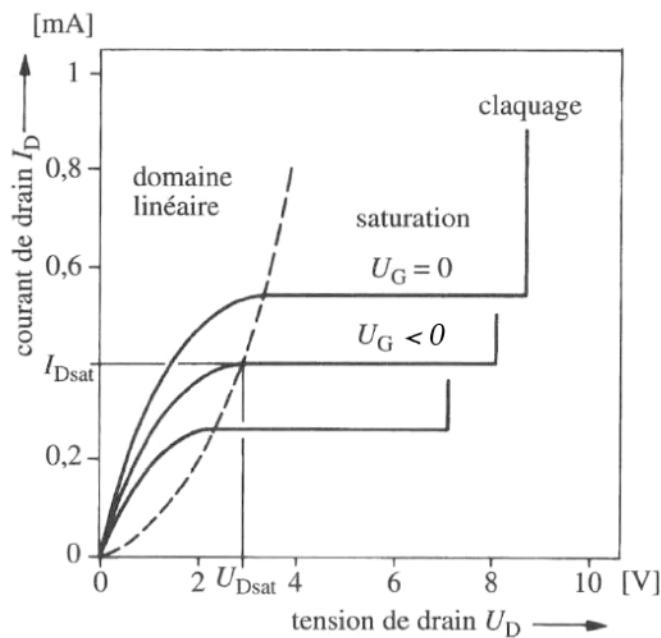
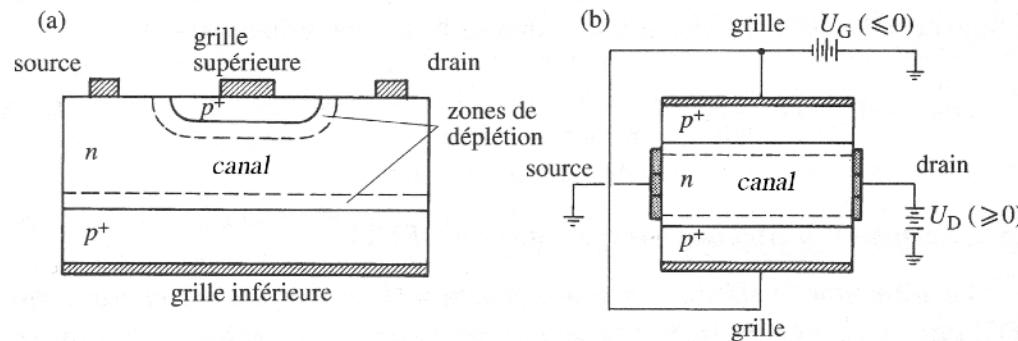
Transistors bipolaires NPN et PNP



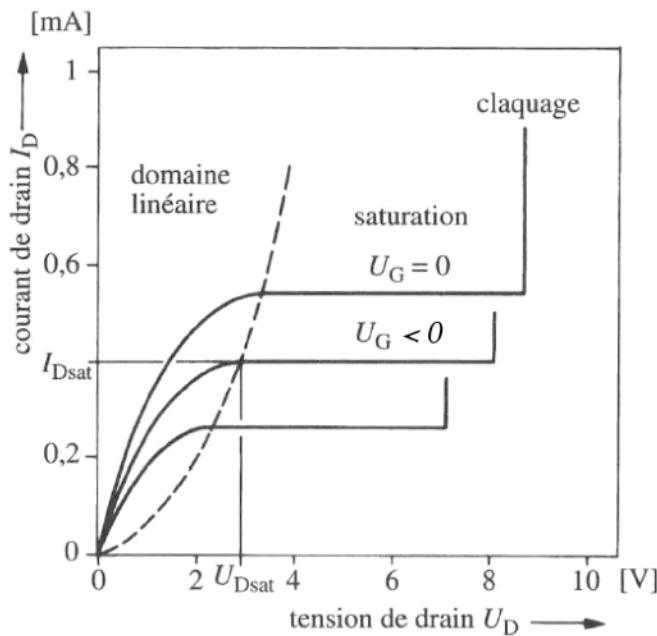
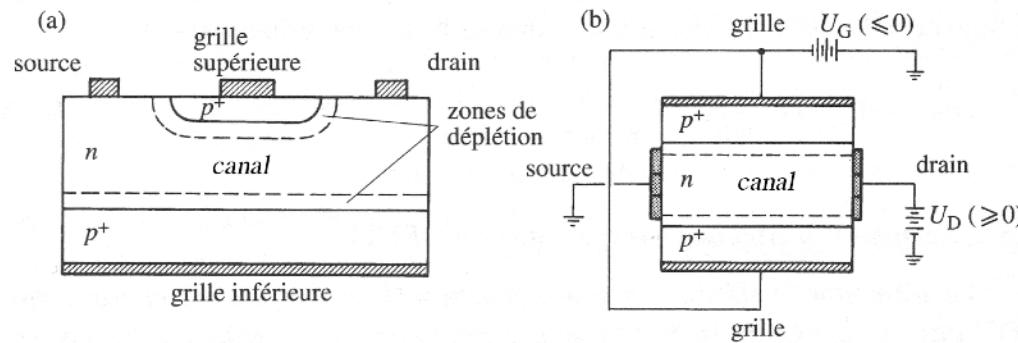
Le transistor comme amplificateur



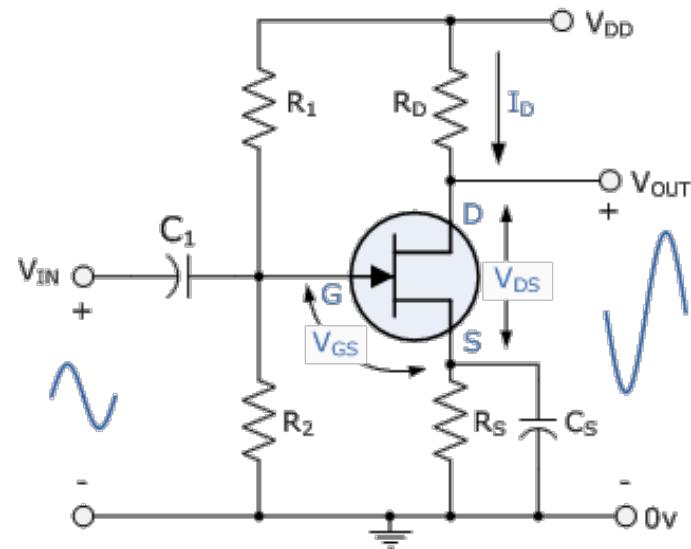
Le transistor J-FET: caractéristiques



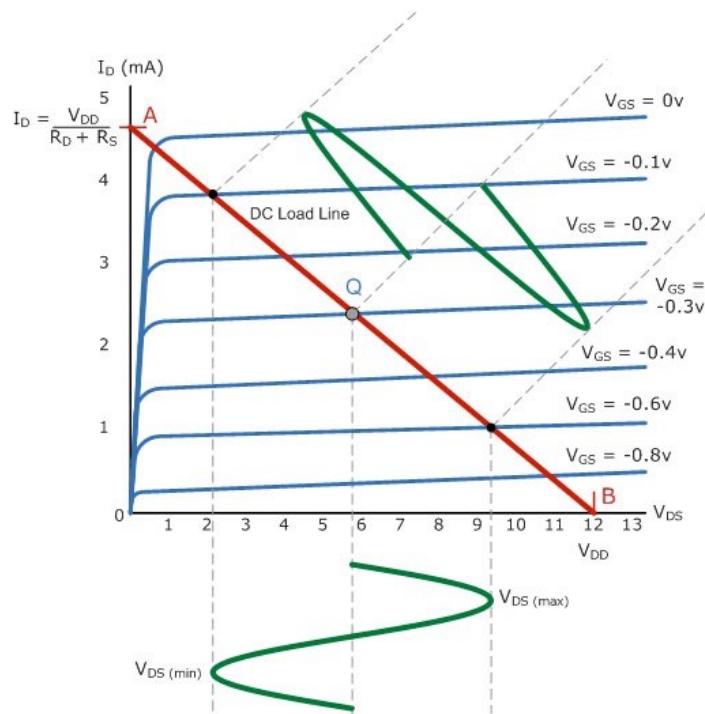
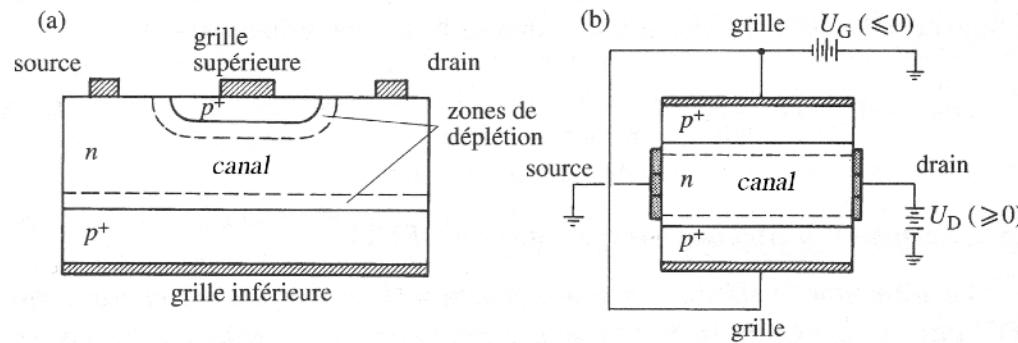
Le transistor J-FET: caractéristiques



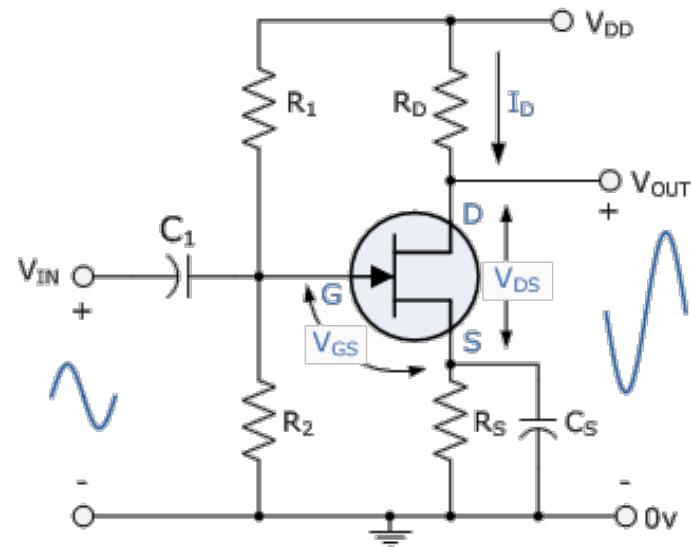
Montage amplificateur



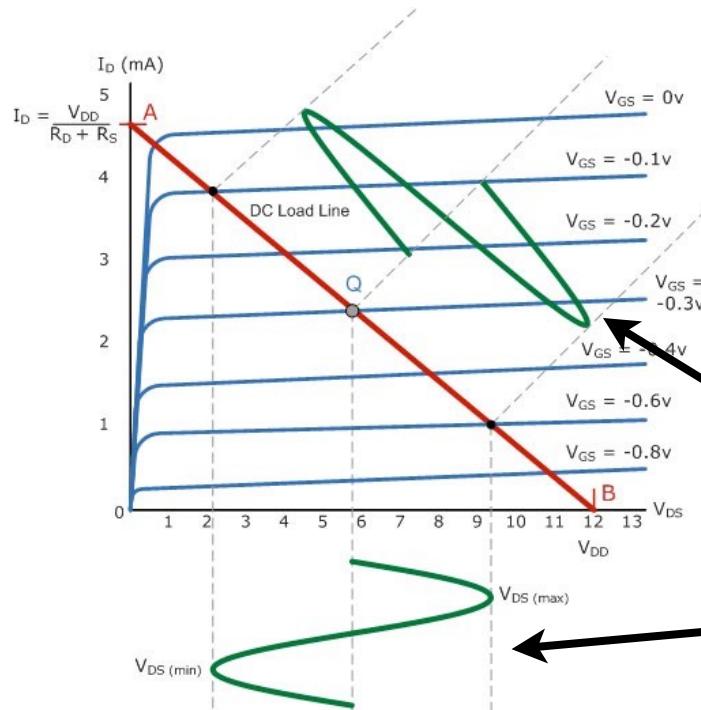
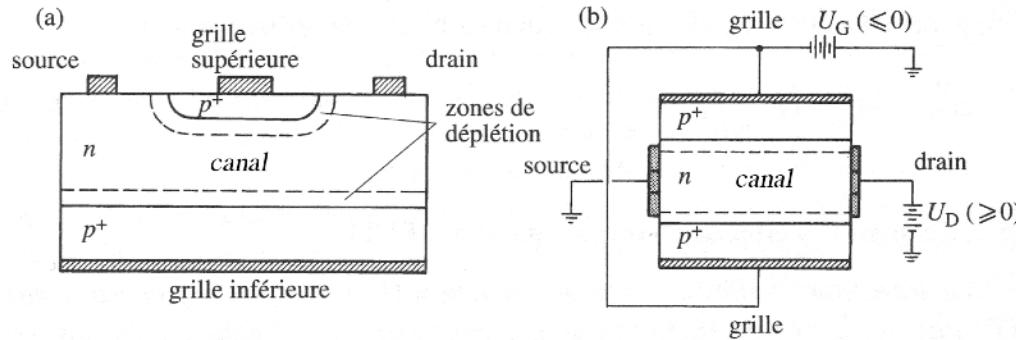
Le transistor J-FET: caractéristiques



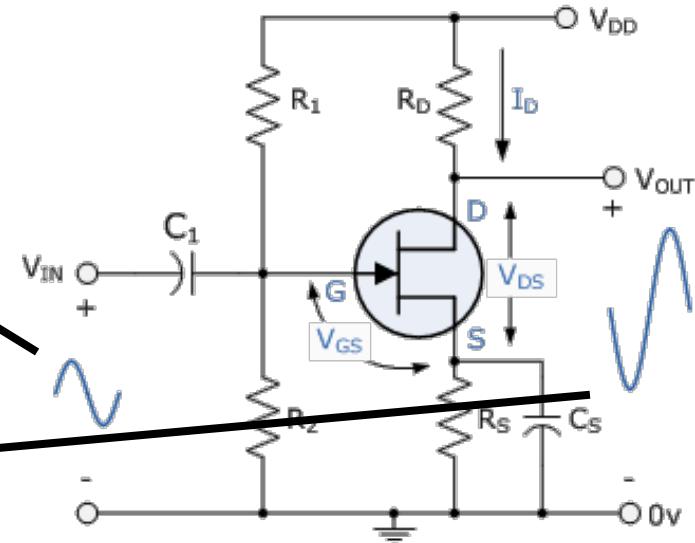
Montage amplificateur



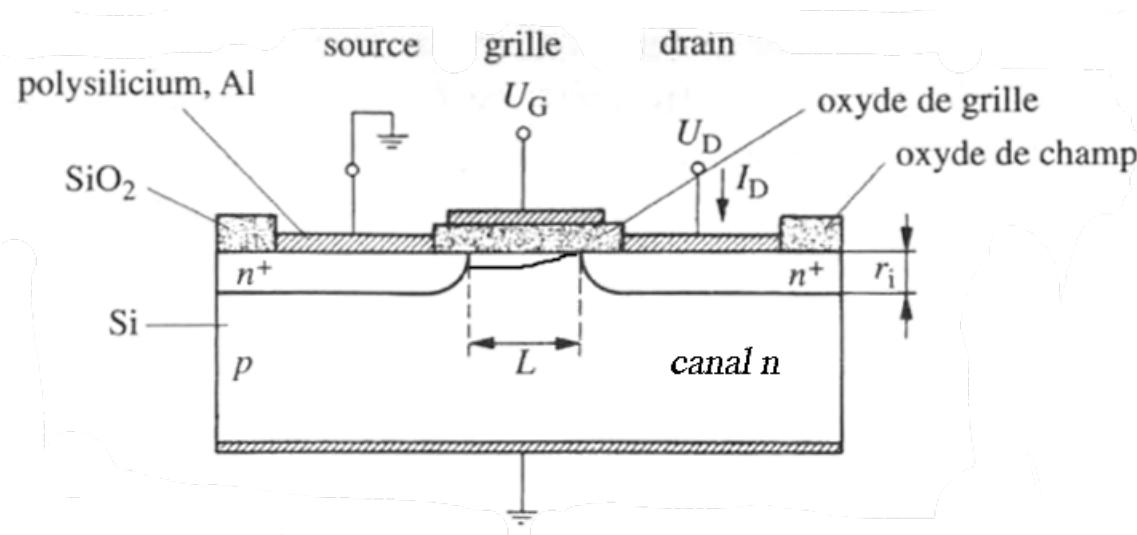
Le transistor J-FET: caractéristiques



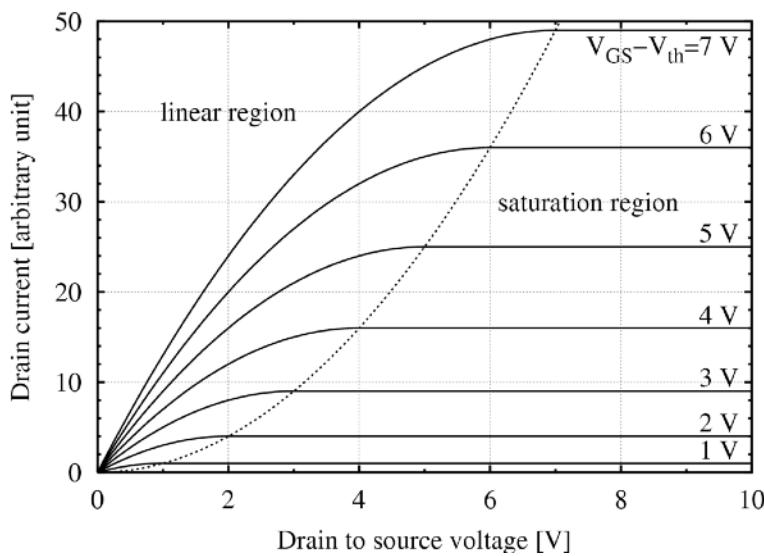
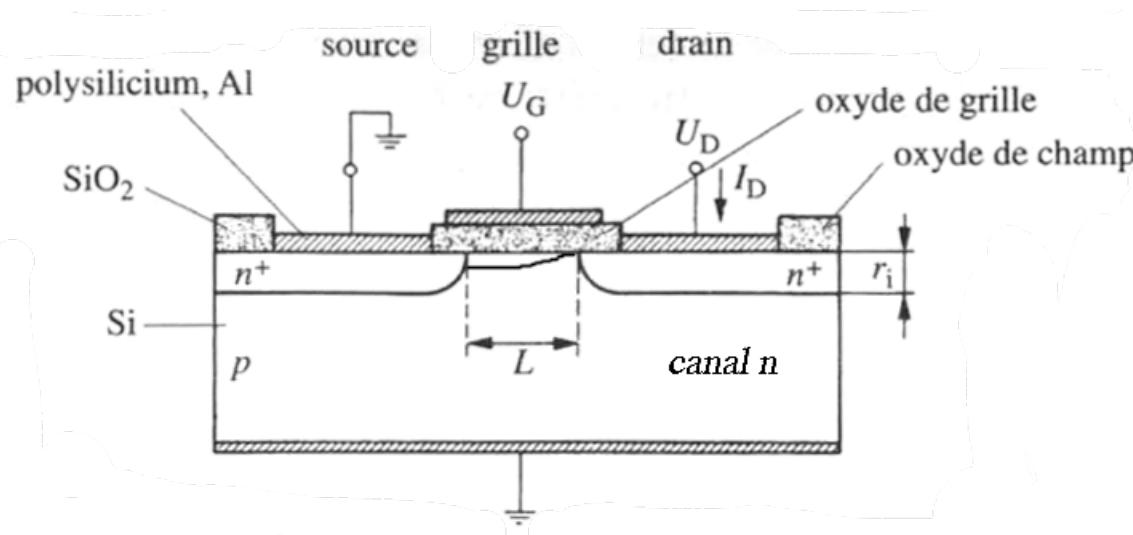
Montage amplificateur



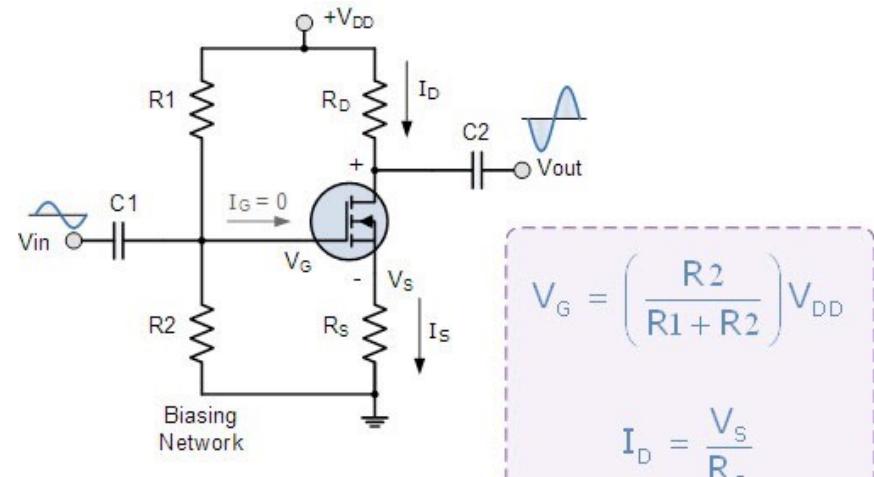
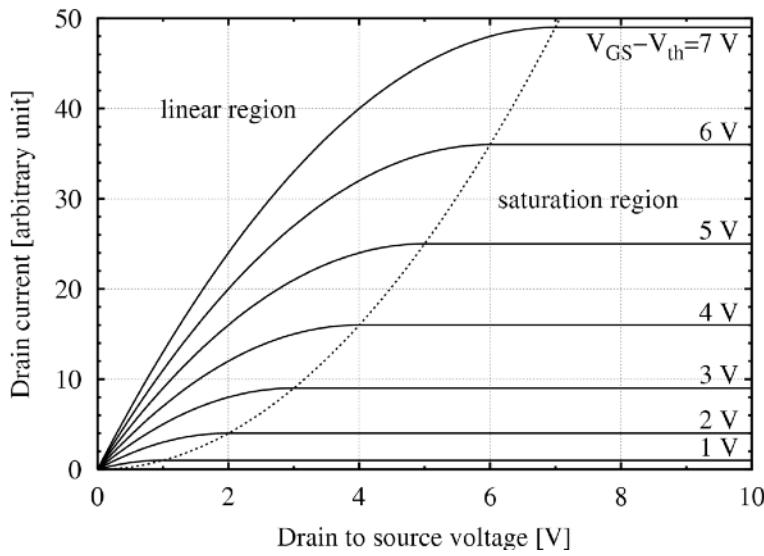
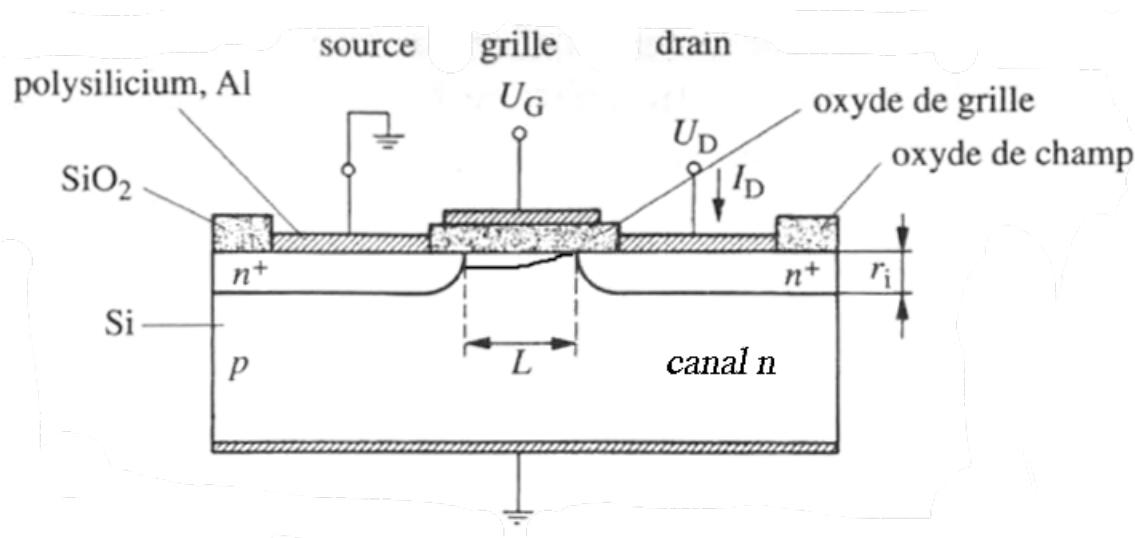
Le transistor MOS - FET



Le transistor MOS - FET



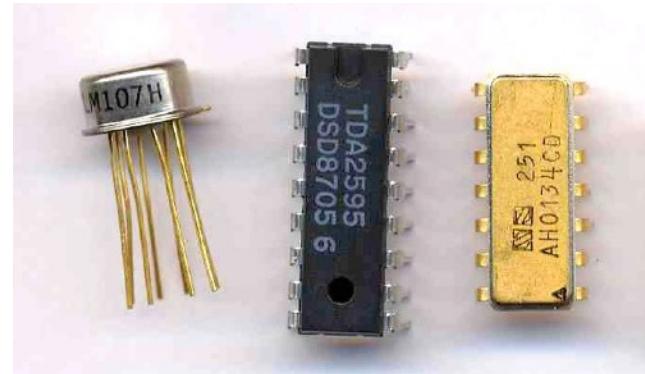
Le transistor MOS - FET



$$V_G = \left(\frac{R_2}{R_1 + R_2} \right) V_{DD}$$

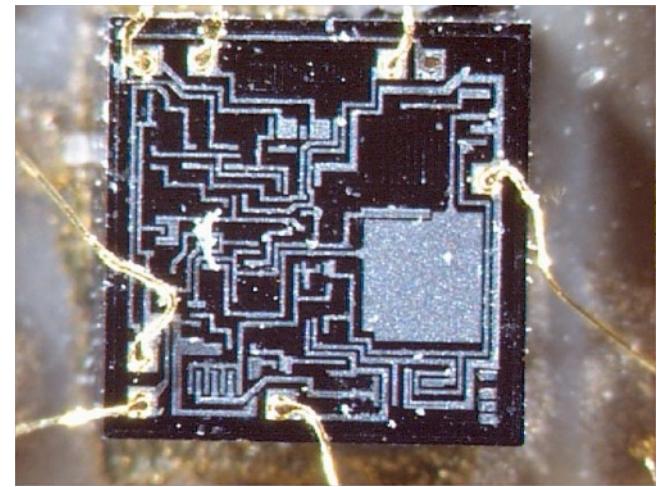
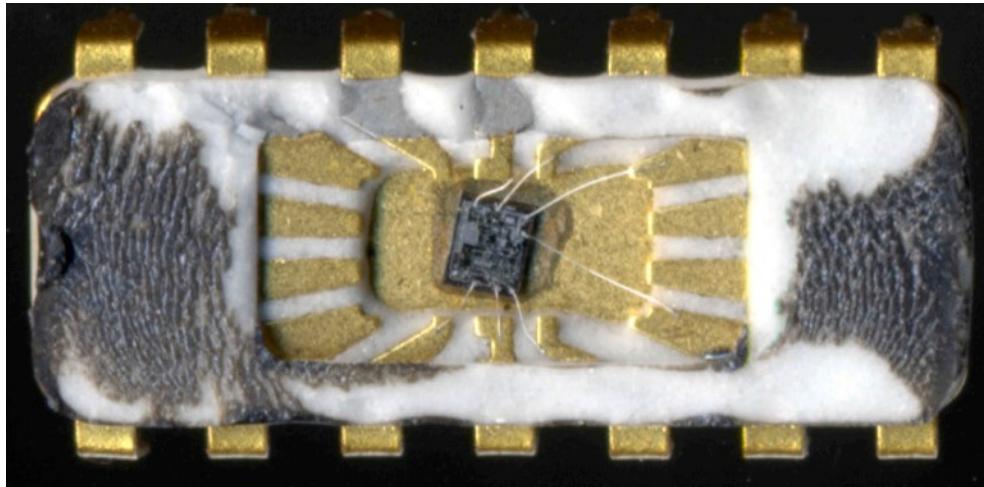
$$I_D = \frac{V_S}{R_S}$$

Fonctions analogiques et circuits intégrés



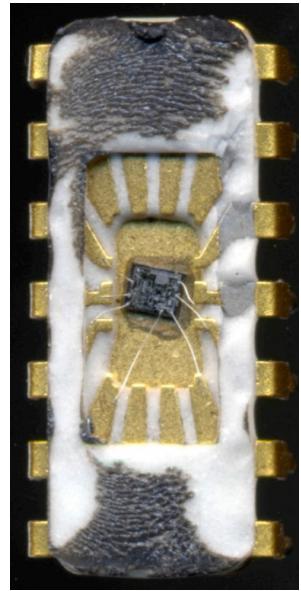
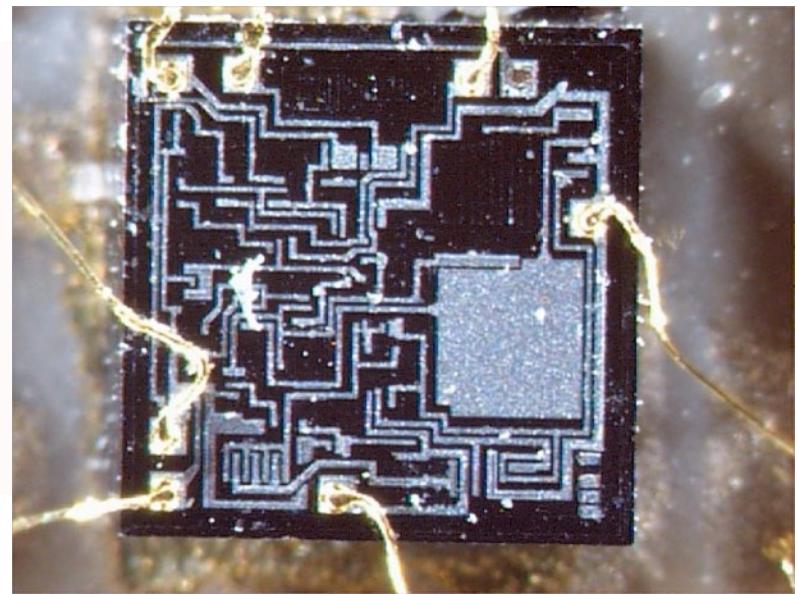
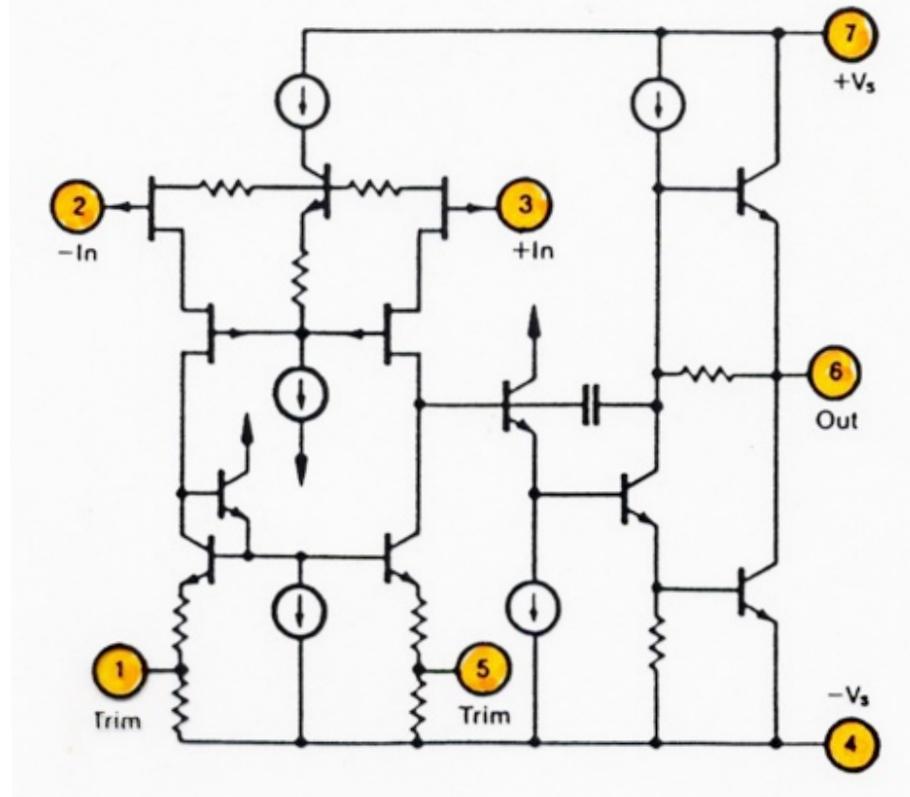
La combinaison d'éléments linéaires (résistances, capacités, inductances), non-linéaires (diodes,...) et actifs (transistors,...) permet de réaliser des circuits électroniques avec des **fonctions analogiques** précises, comme amplificateurs, comparateurs, oscillateurs, modulateurs, etc.

Actuellement, de nombreuses fonctions analogiques sont réalisées par intégration des divers éléments sur un seul substrat de silicium. Ce sont les **circuits intégrés analogiques**.

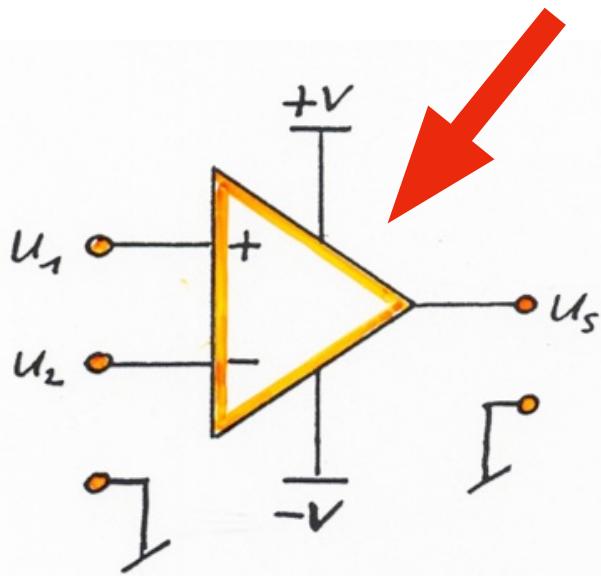
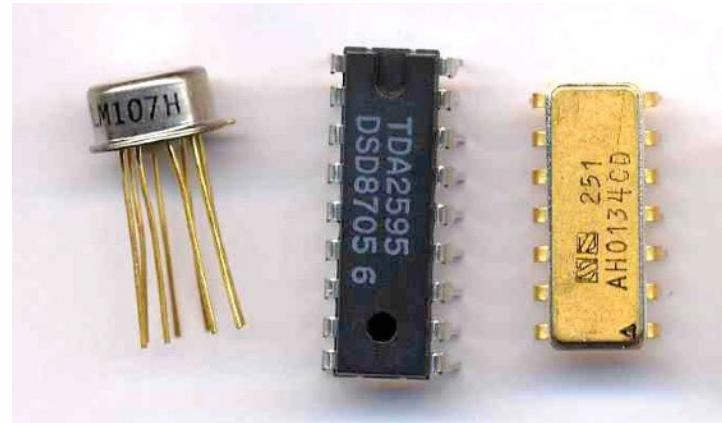
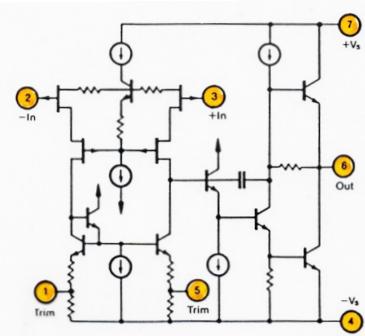


Fonctions analogiques et circuits intégrés

Exemple: ampli opérationnel à entrées FET



Amplis opérationnels



G = gain de l'amplificateur opérationnel

$$u_s = G(u_1 - u_2)$$

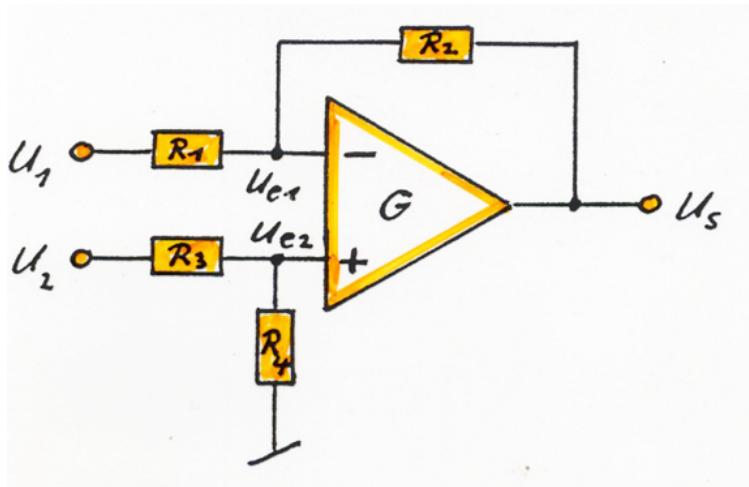
G est très grand (10^4 to 10^6)

L'impédance d'entrée (Z_i) est très grande
(10^6 to $10^9 \Omega$)

L'ampli opérationnel permet de réaliser très simplement, en utilisant exclusivement les équations de Kirchhoff, les équations constitutives des éléments passifs et l'équation de l'ampli opérationnel, une très grande variété de fonctions analogiques, dont on va donner quelques exemples dans la suite.

Circuits linéaires

Amplificateur de tension



Impédance d'entrée $z_i \gg R_i \Rightarrow$

$$u_{e2} = \frac{R_4}{R_3 + R_4} u_2$$

$$u_{e1} = u_1 + \frac{R_1}{R_1 + R_2} (u_s - u_1)$$

$$\text{Gain } G \Rightarrow u_s = G(u_{e2} - u_{e1})$$

$$u_s = G \left(\frac{R_4}{R_3 + R_4} u_2 - u_1 - \frac{R_1}{R_1 + R_2} (u_s - u_1) \right)$$

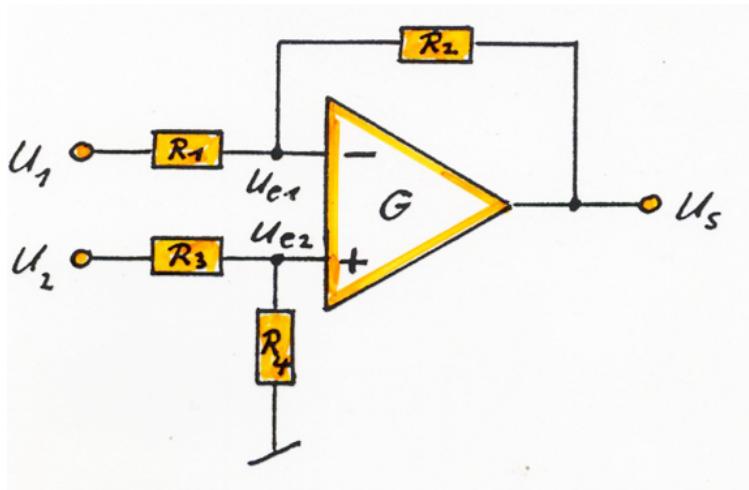
$$\Rightarrow u_s = \frac{\left(\frac{R_4}{R_3 + R_4} u_2 - \frac{R_1}{R_1 + R_2} u_1 \right) G}{1 + \frac{GR_1}{R_1 + R_2}}$$

G très grand \Rightarrow

$$u_s \equiv \frac{R_4(R_1 + R_2)}{(R_3 + R_4)R_1} u_2 - \frac{R_2}{R_1} u_1$$

Circuits linéaires

Amplificateur de tension



Impédance d'entrée $z_i \gg R_i \Rightarrow$

$$u_{e2} = \frac{R_4}{R_3 + R_4} u_2$$

$$u_{e1} = u_1 + \frac{R_1}{R_1 + R_2} (u_s - u_1)$$

$$\text{Gain } G \Rightarrow u_s = G(u_{e2} - u_{e1})$$

$$u_s = G \left(\frac{R_4}{R_3 + R_4} u_2 - u_1 - \frac{R_1}{R_1 + R_2} (u_s - u_1) \right)$$

$$\Rightarrow u_s = \frac{\left(\frac{R_4}{R_3 + R_4} u_2 - \frac{R_1}{R_1 + R_2} u_1 \right) G}{1 + \frac{GR_1}{R_1 + R_2}}$$

G très grand \Rightarrow

$$u_s \equiv \frac{R_4(R_1 + R_2)}{(R_3 + R_4)R_1} u_2 - \frac{R_2}{R_1} u_1$$

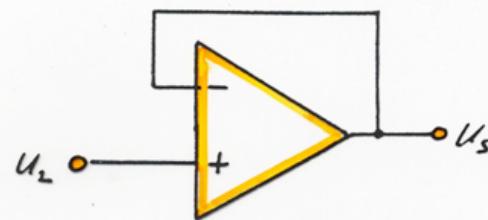
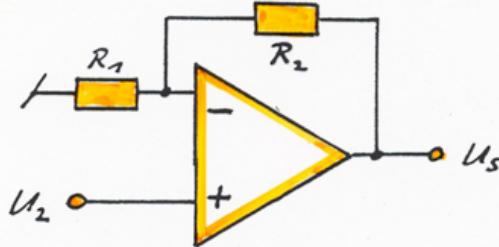
Amplificateur différentiel

$$\frac{R_1}{R_2} = \frac{R_3}{R_4} \quad \Rightarrow$$

$$u_s = \frac{R_2}{R_1} (u_2 - u_1)$$

Circuits linéaires

Amplificateur non-inverseur



$$u_s \equiv \frac{R_4(R_1 + R_2)}{(R_3 + R_4)R_1} u_2 - \frac{R_2}{R_1} u_1$$

$$\left. \begin{array}{l} R_3 = 0 \text{ and } R_4 \rightarrow \infty \\ u_1 = 0 \end{array} \right\} \Rightarrow$$

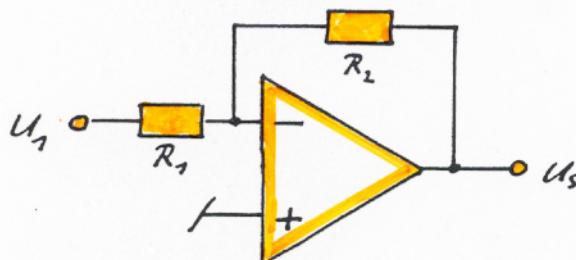
$$u_s = \frac{R_1 + R_2}{R_1} u_2$$

$$R_1 \rightarrow \infty \text{ and } R_2 = 0 \Rightarrow$$

$$u_s = u_2$$

Ces deux amplificateurs ont une grande impedance d'entrée (!)

Amplificateur inverseur

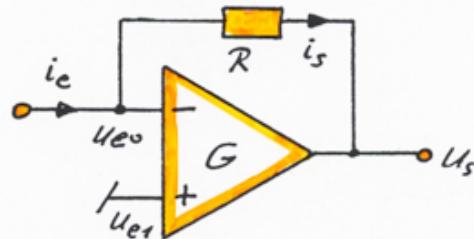


$$R_3 = R_4 = 0 \text{ and } u_2 = 0 \Rightarrow$$

$$u_s = -\frac{R_2}{R_1} u_1$$

Circuits linéaires

“Amplificateur piloté en courant”



Impédance d'entrée : $z_i \gg R \Rightarrow$

$$i_s \cong i_e$$

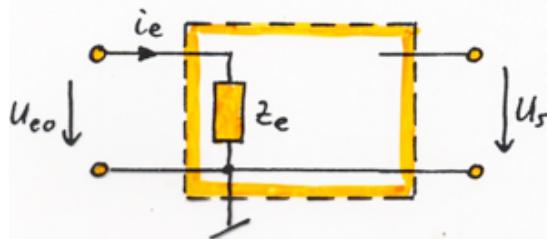
$$u_{eo} - u_s = Ri_s = Ri_e$$

$$\Rightarrow u_{e1} = 0$$

$$u_s = G(u_{e1} - u_{eo}) = -G(u_s + Ri_e)$$

$$G \gg 1 \quad \Rightarrow$$

$$u_s = \frac{-GRi_e}{1+G} \cong -Ri_e$$



Impédance d'entrée vue par la source :

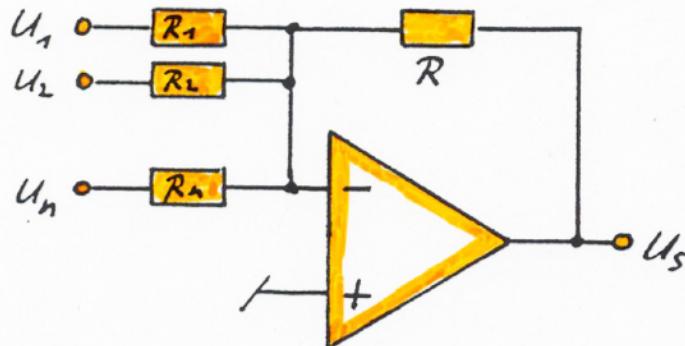
$$z_e = \frac{u_{eo}}{i_e} = \frac{u_s + Ri_e}{i_e} = \left(1 - \frac{G}{1+G}\right)R$$

$$z_e = \frac{1}{1+G}R$$

Comme G est très grand, z_e est petit ($z_e \ll R$)

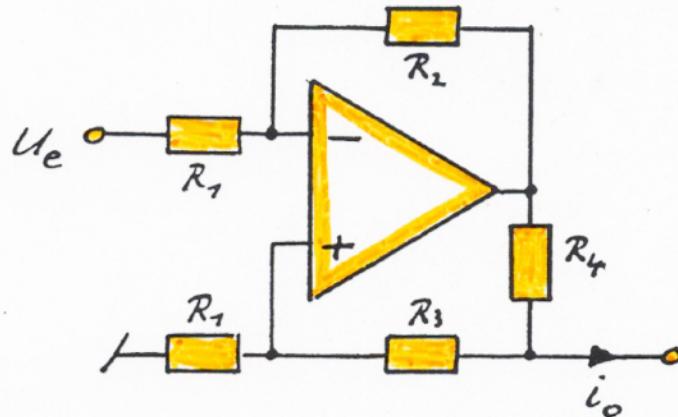
Circuits linéaires

Amplificateur sommateur



$$u_s = -R \sum_{i=1}^n \frac{u_i}{R_i}$$

Source de courant pilotée en tension

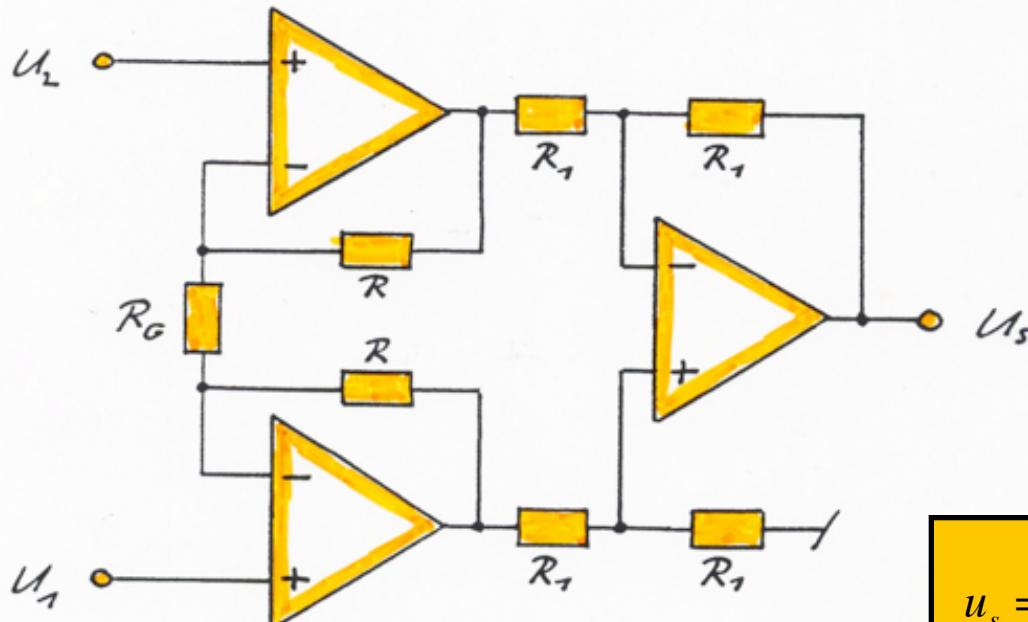


$$\text{si } \begin{cases} R_2 = R_3 + R_4 \\ R_4 \gg R_3 \end{cases}$$

$$i_o = \frac{R_2}{R_1 R_4} u_e$$

Circuits linéaires

Amplificateur différentiel d'instrumentation



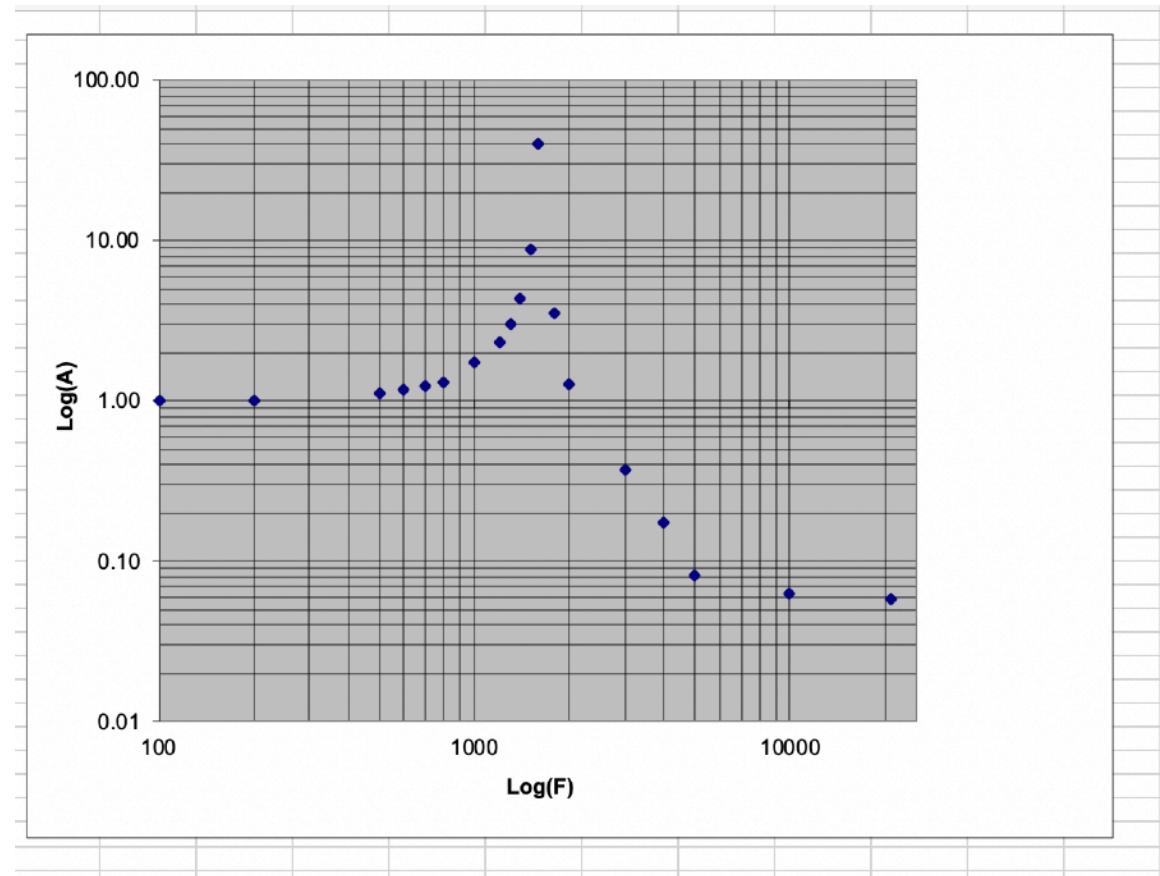
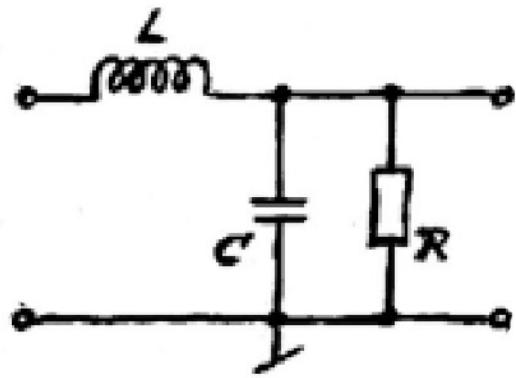
$$u_s = \left(1 + \frac{R_2}{R_1 R_4}\right)(u_1 - u_2)$$

L'impédance d'entrée z_i peut être très grande

($z_i \approx 1 \times 10^{12} \Omega$ pour des transistors FET)

Le gain peut aller de 1 ($R_G \rightarrow \infty$) à des milliers.

FILTRAGE

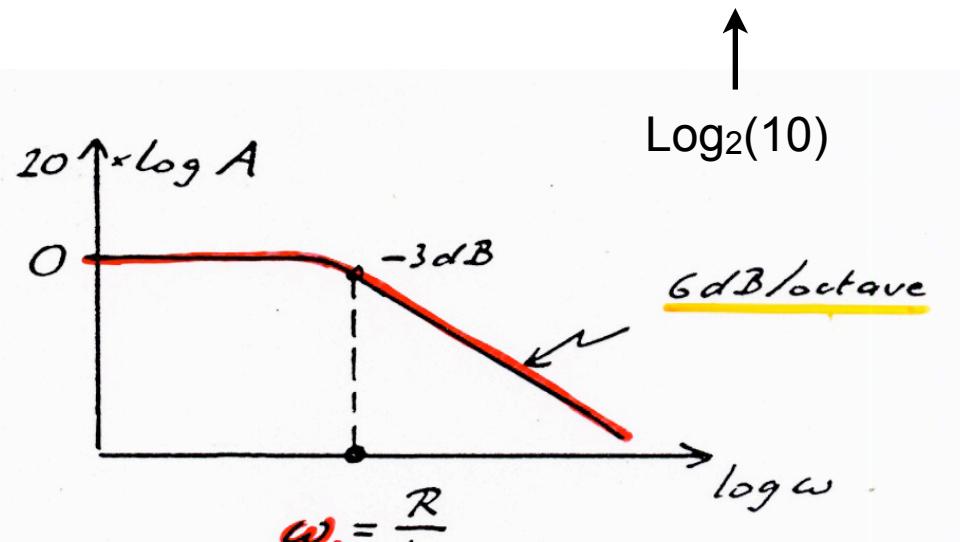
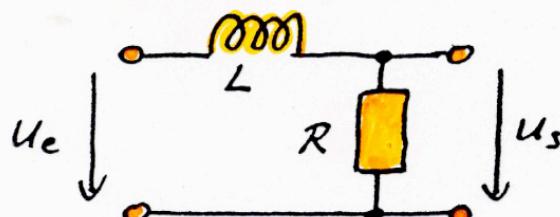


Les filtres passifs

Filtres passe-bas

Note: $6 \text{ dB/octave} = 20 \text{ dB/décade}$
Ou $\text{dB/décade} = 3.32 \text{ dB/octave}$

1er ordre

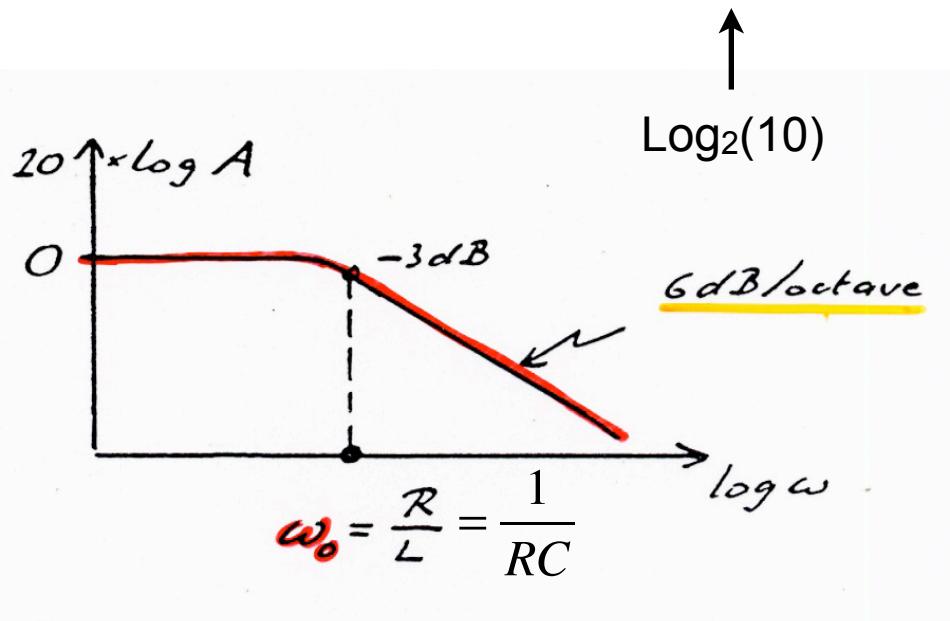
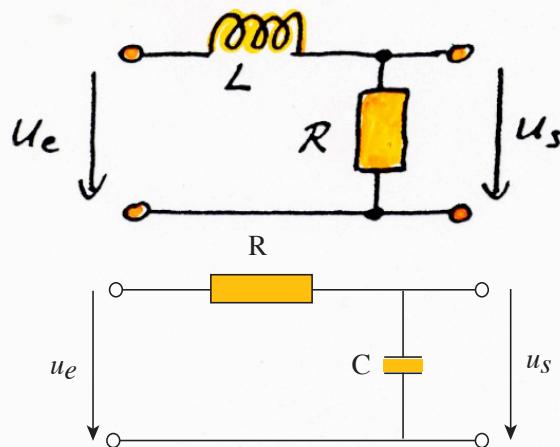


Les filtres passifs

Note: $6 \text{ dB/octave} = 20 \text{ dB/décade}$
Ou $\text{dB/décade} = 3.32 \text{ dB/octave}$

Filtres passe-bas

1er ordre

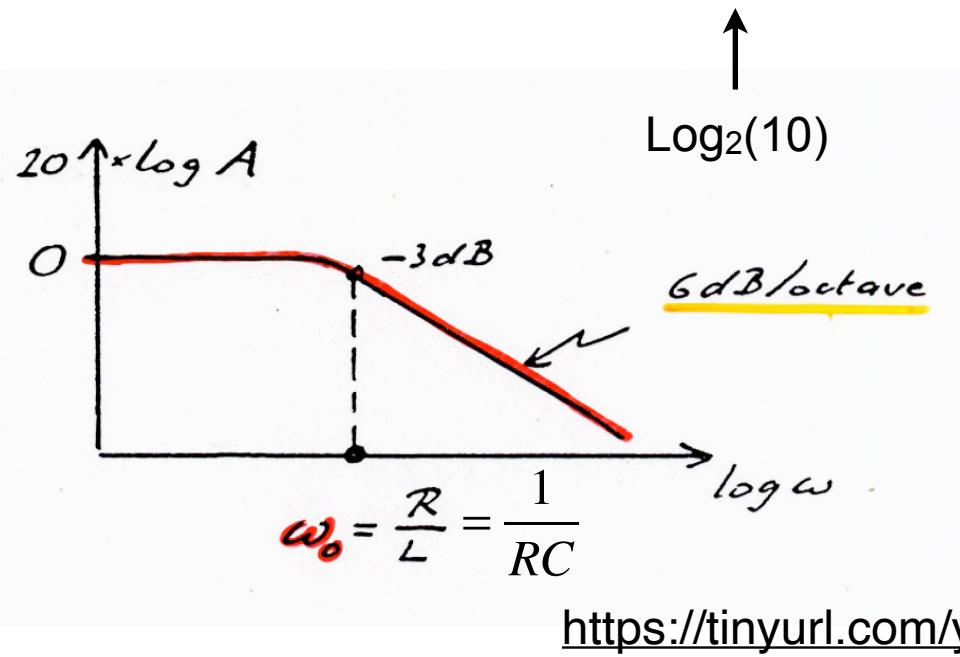
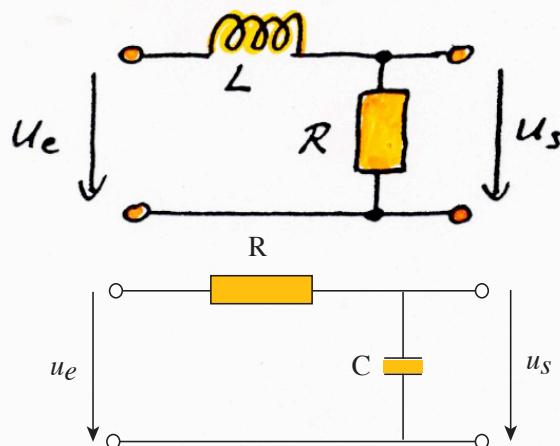


Les filtres passifs

Filtres passe-bas

Note: $6 \text{ dB/octave} = 20 \text{ dB/décade}$
Ou $\text{dB/décade} = 3.32 \text{ dB/octave}$

1er ordre



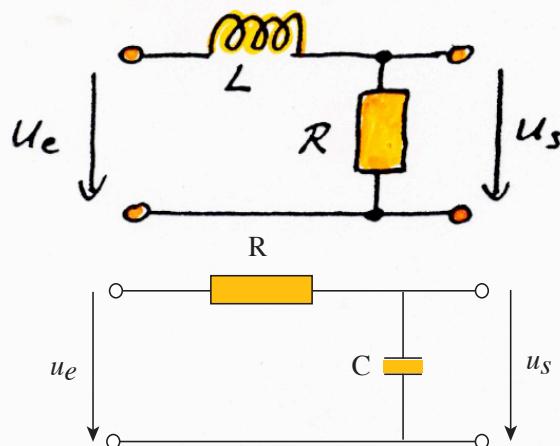
<https://tinyurl.com/yerd6sd7>

Les filtres passifs

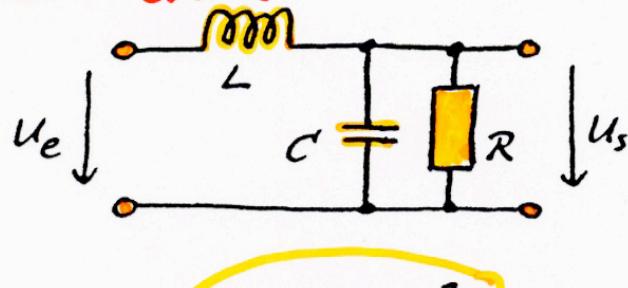
Filtres passe-bas

Note: $6 \text{ dB/octave} = 20 \text{ dB/décade}$
Ou $\text{dB/décade} = 3.32 \text{ dB/octave}$

1^{er} ordre



2^{ème} ordre



$$L = 4CR^2$$

$20 \times \log A$

$\text{Log}_2(10)$

$$\omega_0 = \frac{R}{L} = \frac{1}{RC}$$

<https://tinyurl.com/yerd6sd7>

$20 \times \log A$

12 dB/octave

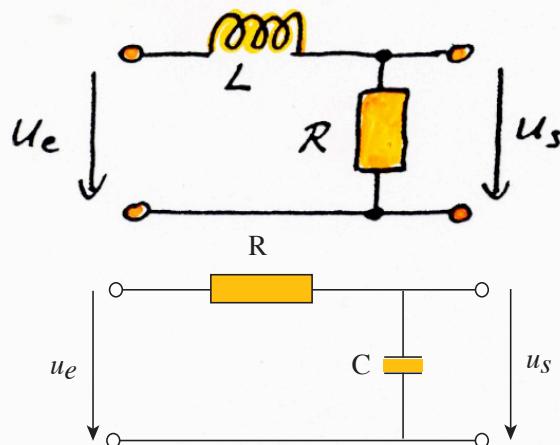
$$\omega_0 = \frac{1}{\sqrt{LC}}$$

Les filtres passifs

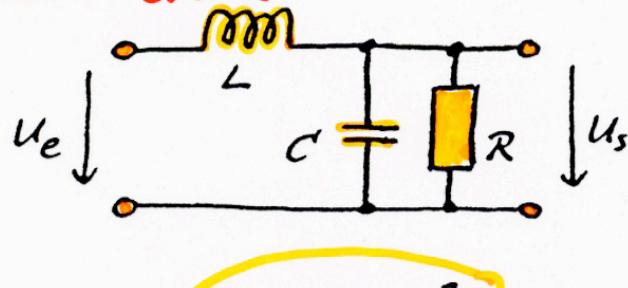
Filtres passe-bas

Note: $6 \text{ dB/octave} = 20 \text{ dB/décade}$
Ou $\text{dB/décade} = 3.32 \text{ dB/octave}$

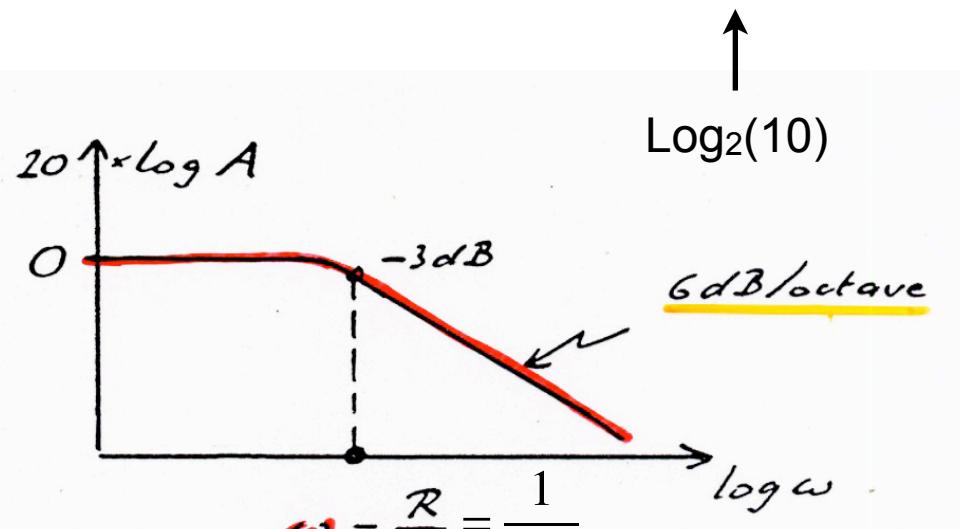
1^{er} ordre



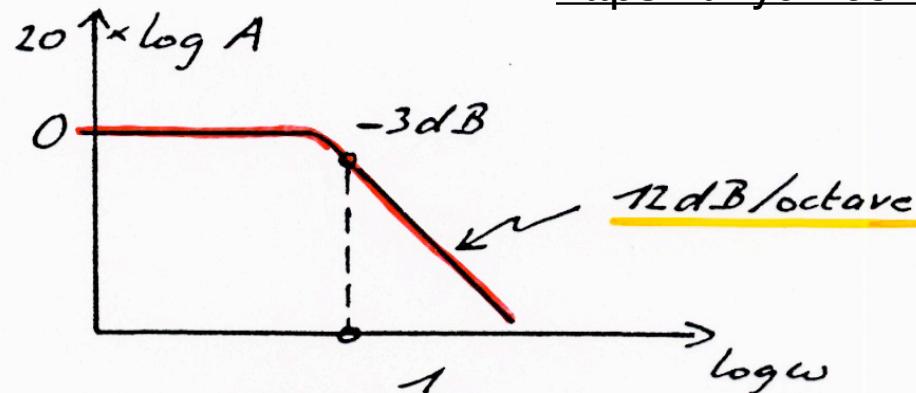
2^{ème} ordre



$$L = 4CR^2$$



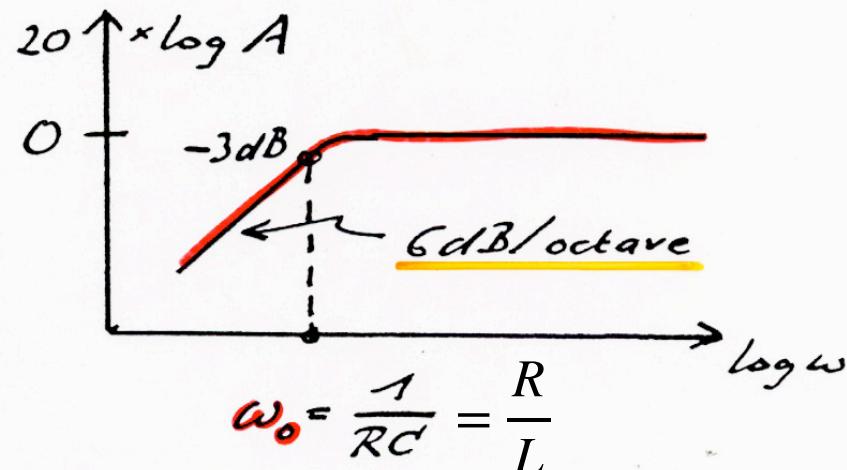
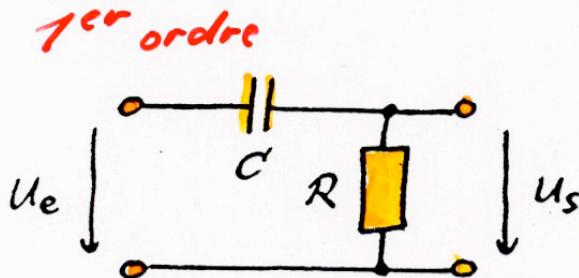
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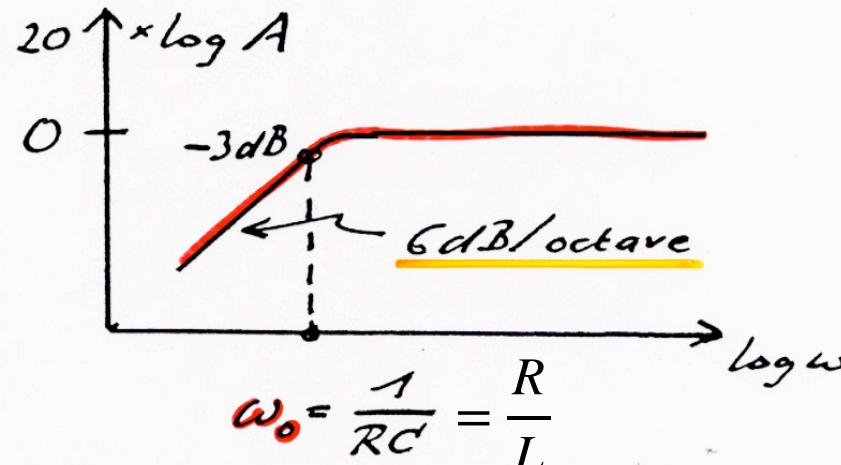
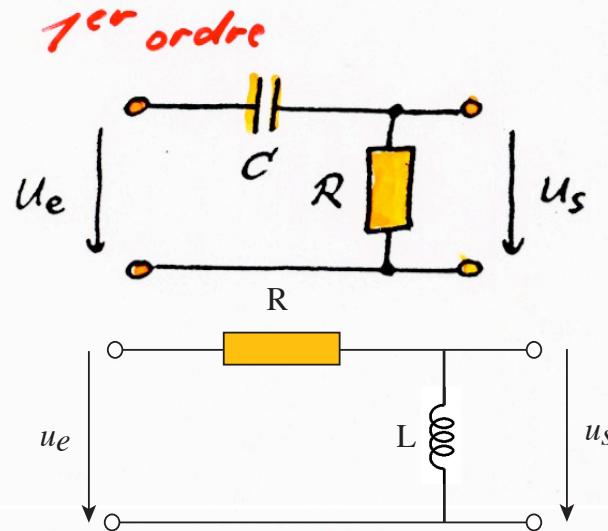
Les filtres passifs

Filtres passe-haut



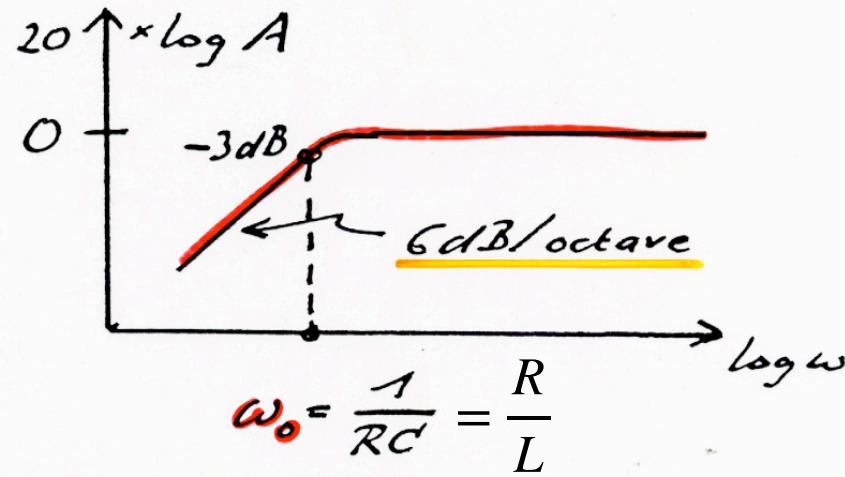
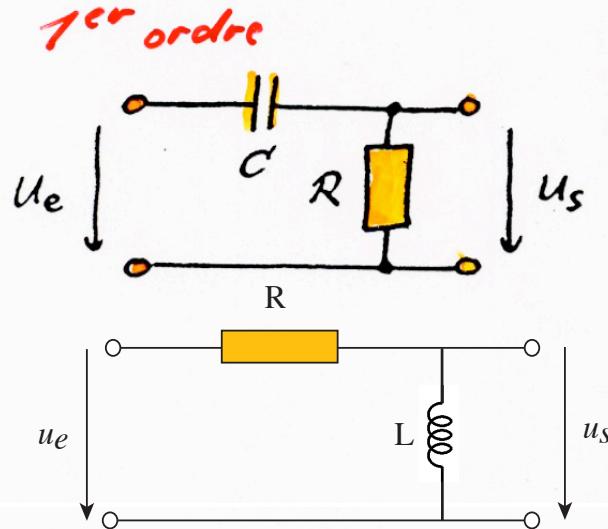
Les filtres passifs

Filtres passe-haut



Les filtres passifs

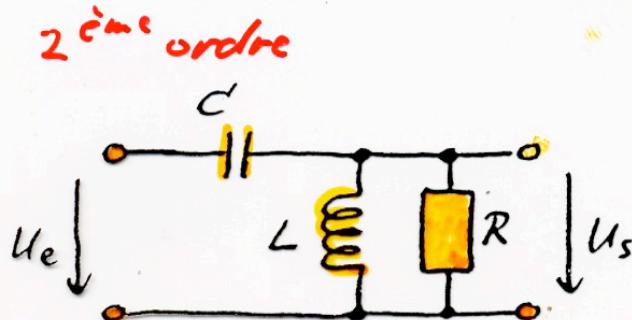
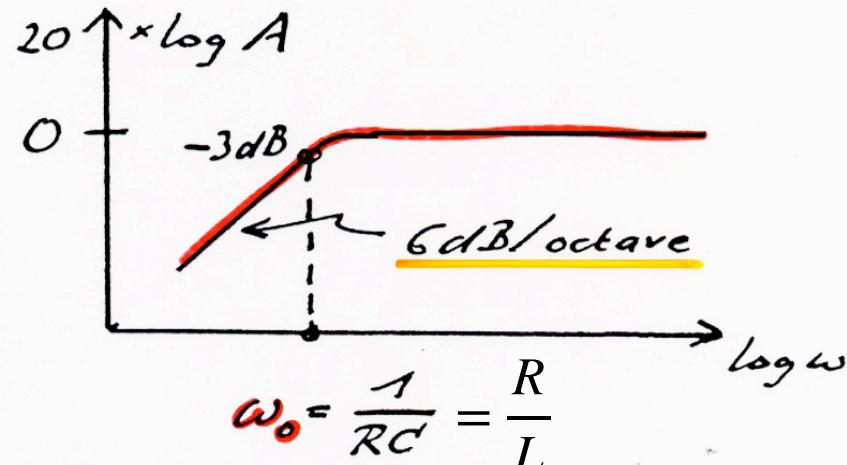
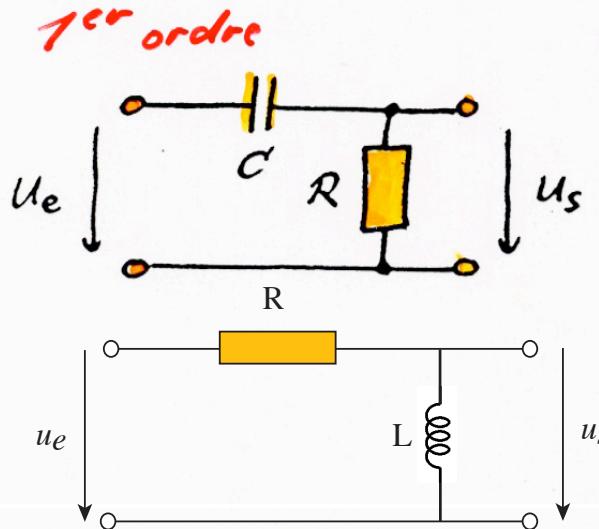
Filtres passe-haut



<https://tinyurl.com/yzmmwbt6>

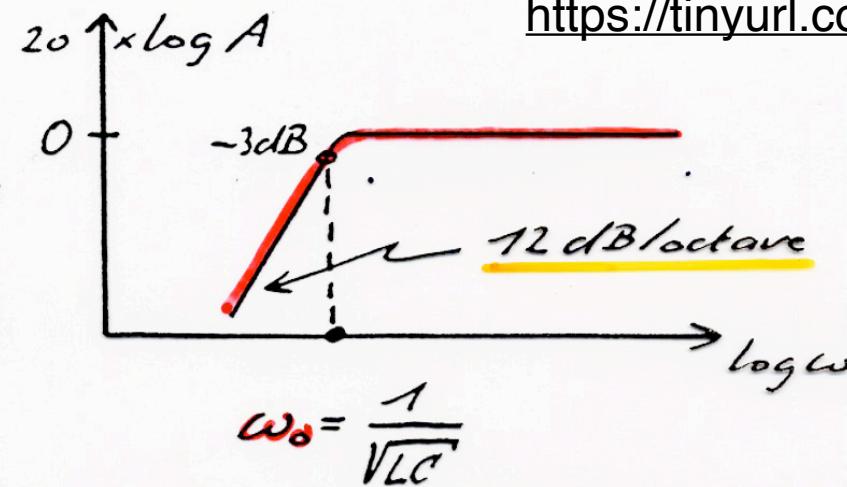
Les filtres passifs

Filtres passe-haut



$$L = 4CR^2$$

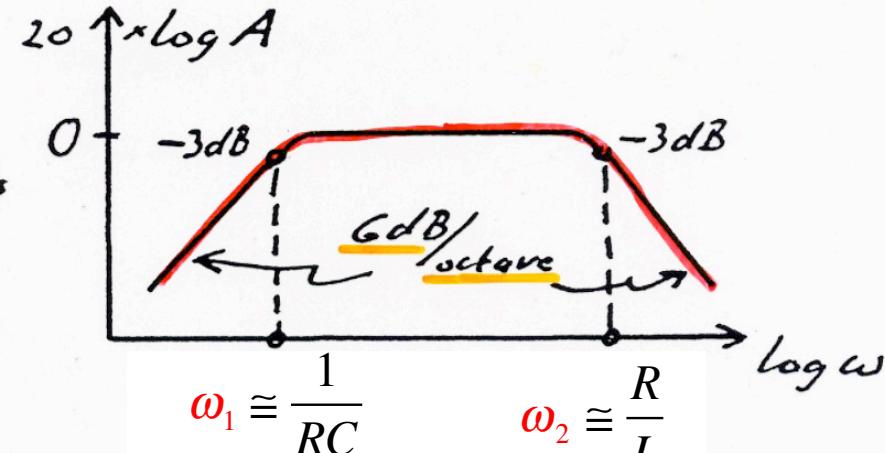
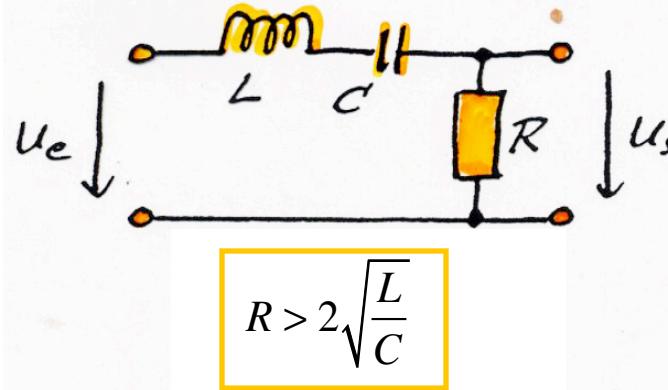
Amortissement critique



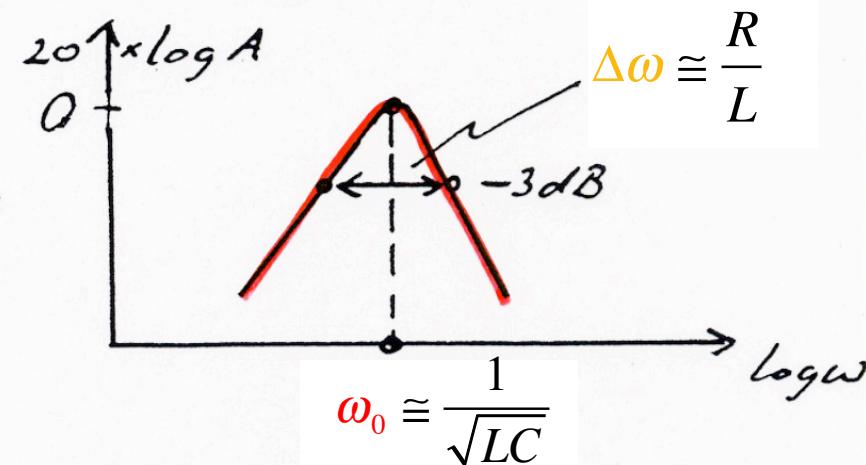
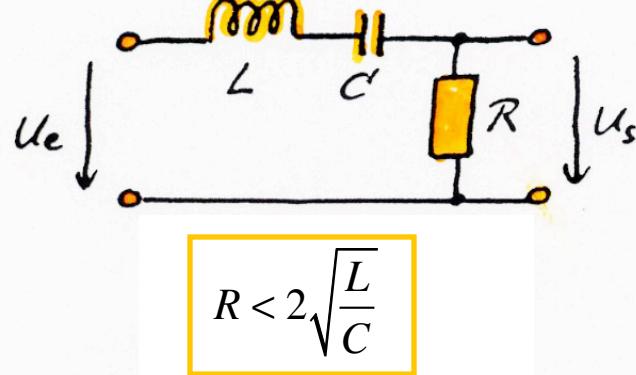
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Les filtres passifs

Filtre passe-bande

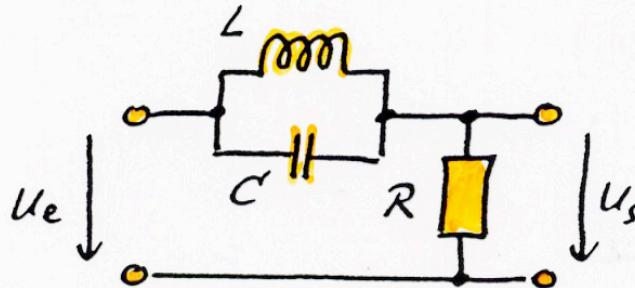


Filtre résonnant

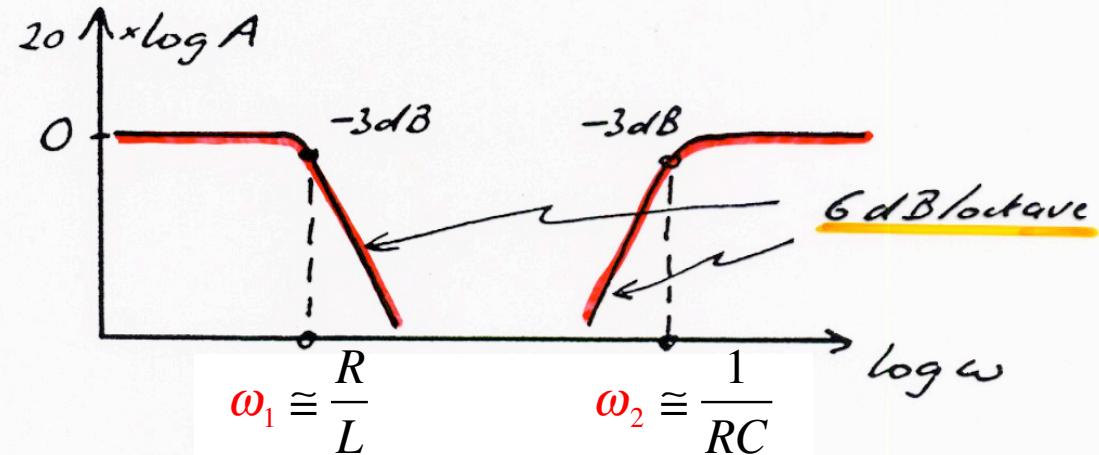


Filtres passifs

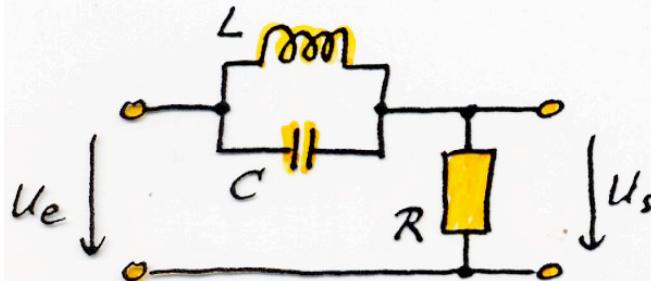
Filtre coupe-bande



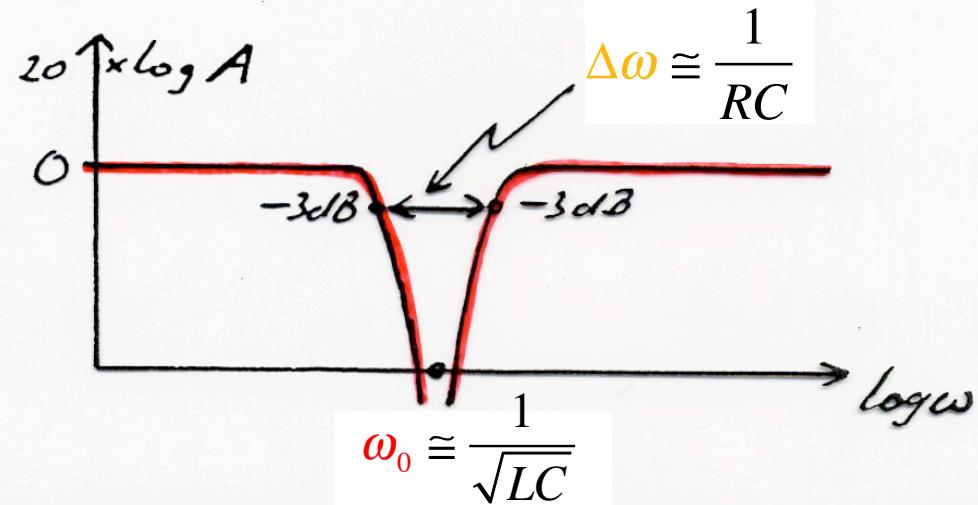
$$R < \frac{1}{2} \sqrt{\frac{L}{C}}$$



Filtre bouchon

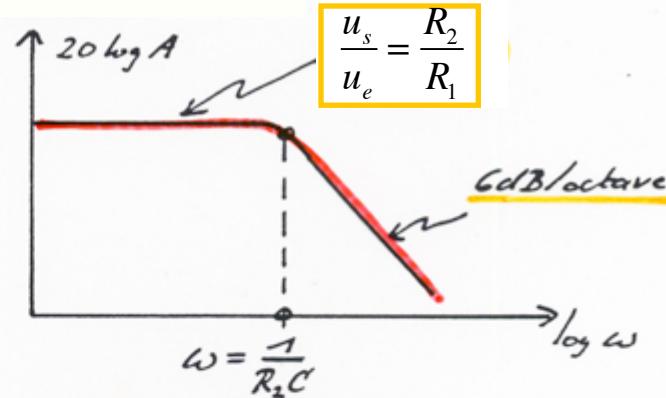
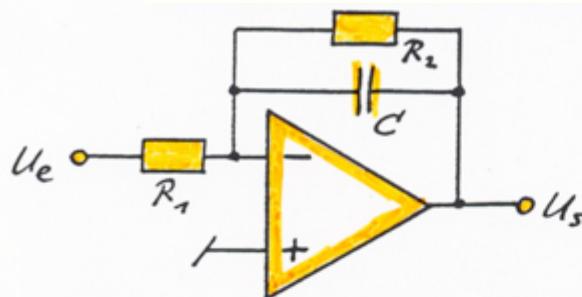


$$R > \frac{1}{2} \sqrt{\frac{L}{C}}$$



Circuits linéaires

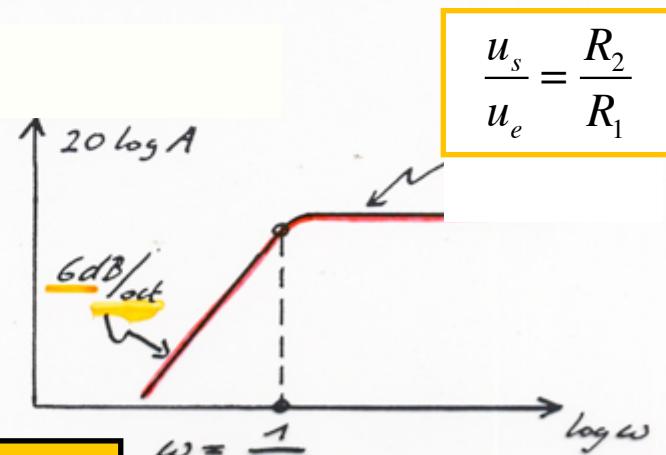
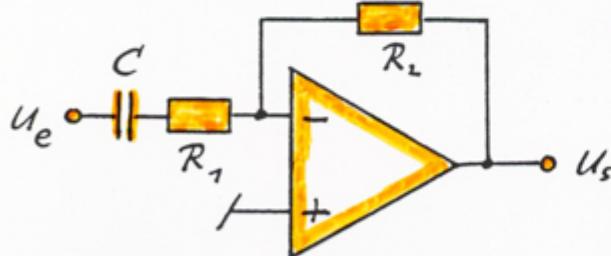
Filtre passe-bas / intégrateur



si $R_2 \rightarrow \infty$ \Rightarrow

$$u_s = -\frac{1}{RC} \int u_e dt$$

Filtre passe-haut / différentiateur

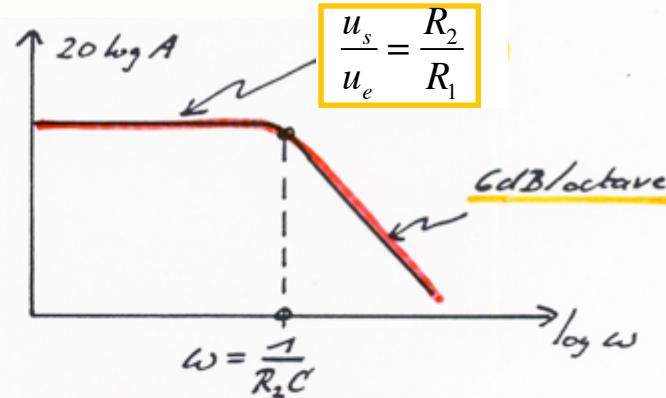
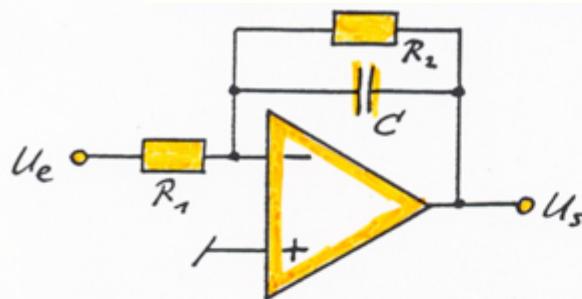


si $R_1 \rightarrow 0$ \Rightarrow

$$u_s = -R_2 C \frac{du_e}{dt}$$

Circuits linéaires

Filtre passe-bas / intégrateur

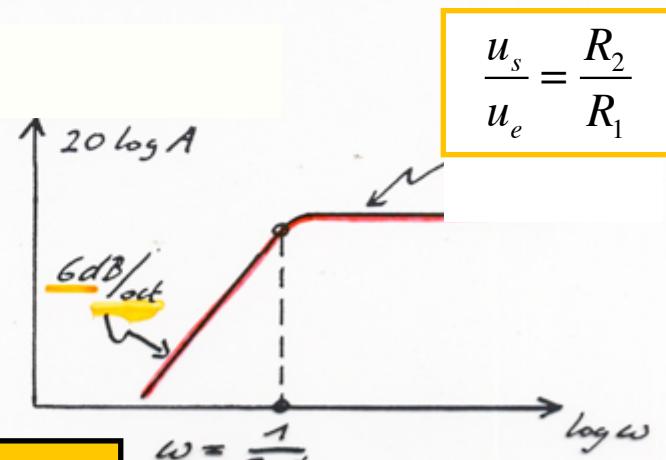
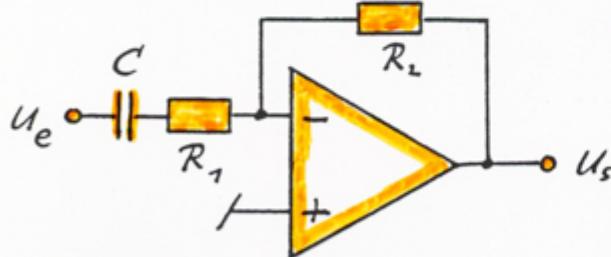


<https://tinyurl.com/yzngnrbm>

$$\text{si } R_2 \rightarrow \infty \Rightarrow$$

$$u_s = -\frac{1}{R_1 C} \int u_e dt$$

Filtre passe-haut / différentiateur



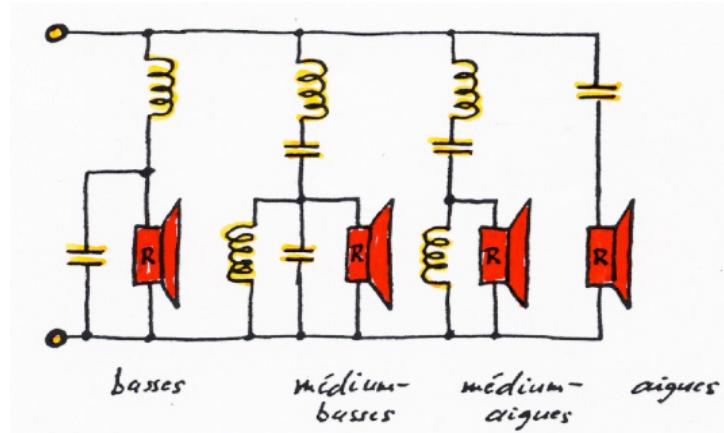
$$\text{si } R_1 \rightarrow 0 \Rightarrow u_s = -R_2 C \frac{du_e}{dt}$$

Circuits - II

Dipôles et quadripôles

D. Mari

EPFL



Le décibel (dB): niveau de pression ou de puissance acoustique

En acoustique, la force d'un son se mesure en décibels (dB). C'est une unité qui utilise le logarithme soit de la puissance du son, elle-même exprimée en Watts par mètre carré W/m^2 ou bien de la différence de pression produite dans le milieu, exprimée en Pascals par mètre carré Pa/m^2 . Mais attention, la notion de puissance sonore ne donne qu'une vague idée du volume perçu par l'humain, car il faut prendre en compte la sensibilité de l'oreille, qui varie principalement selon la fréquence du son. En fait, l'oreille est moins sensible aux basses fréquences.

0 dB correspond au minima que l'oreille humaine peut percevoir appelé seuil d'audibilité, et non au silence absolu. Cette valeur a été choisie par l'expérience, elle vaut $10^{-12} \text{ W} \cdot \text{m}^{-2}$ pour un son de fréquence 1000 Hz, mais la plupart des personnes ont un seuil d'audibilité supérieur à 0 dB (environ 4 dB).

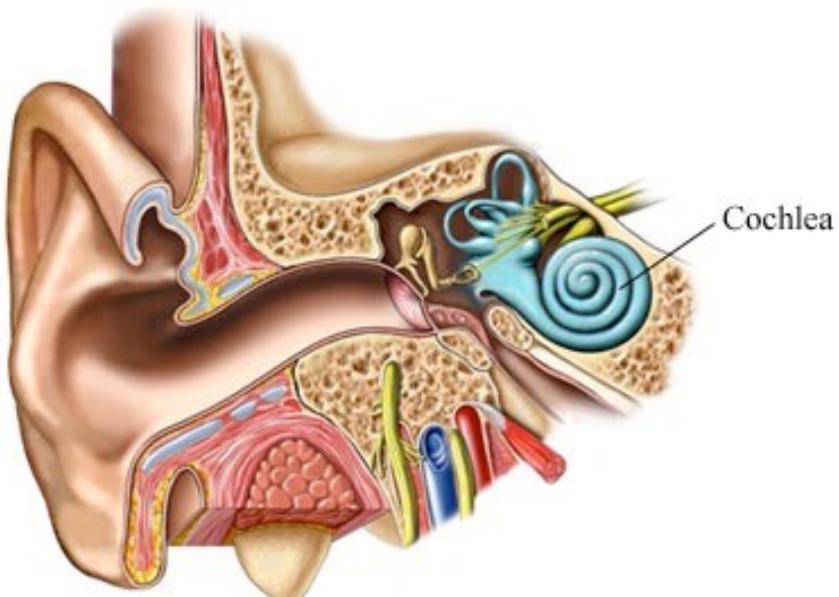
Il suffit de changer la référence de puissance ou de pression (P_0 ou W_0 dans les formules ci-dessous) pour que l'échelle des volumes soit complètement changée. C'est pourquoi les décibels gradués sur le bouton de volume d'une chaîne Hi-Fi ne correspondent pas du tout à des niveaux acoustiques mais à des puissances électriques de sortie de l'amplificateur, ce qui n'a quasiment rien à voir, la valeur 0 dB représentant bien souvent la puissance maximale que l'amplificateur est capable de délivrer.

$$L_p = 10 \log_{10} \left(\frac{p}{p_0} \right)^2 = 20 \log_{10} \frac{p}{p_0}$$

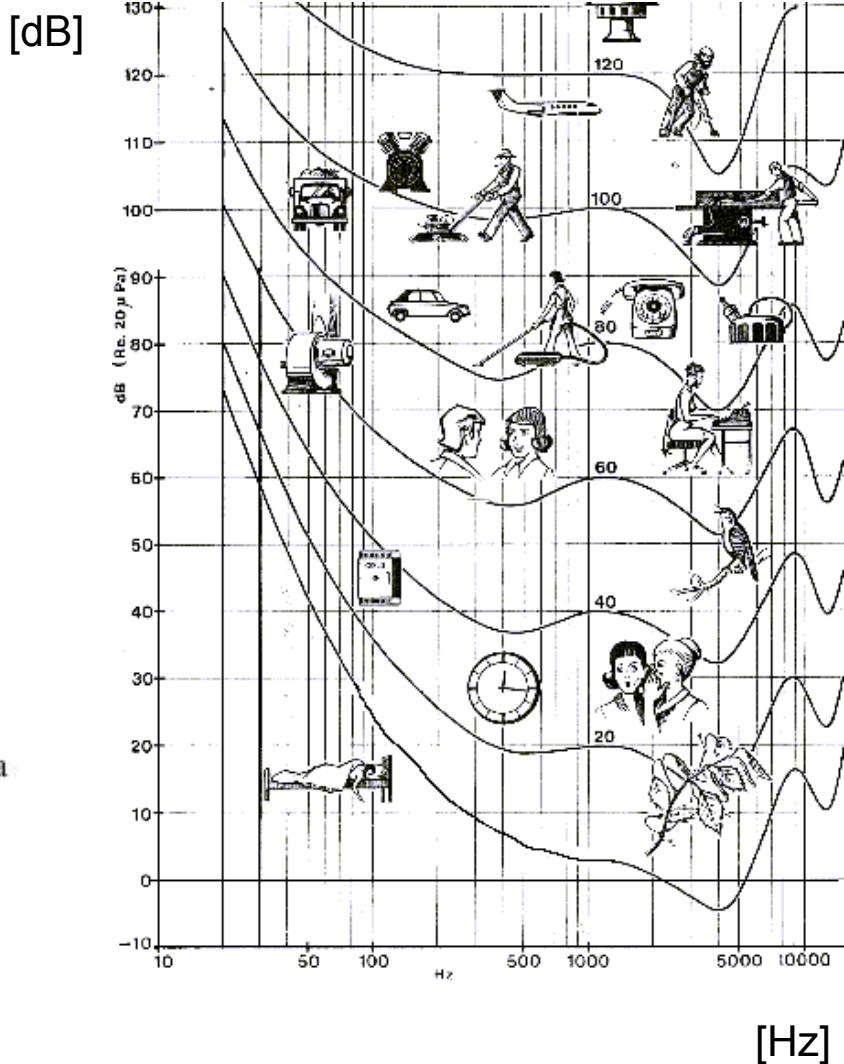
$$L_W = 10 \log_{10} \frac{W}{W_0}$$

| Puissance (W) | Niveau dB | Exemple | Puissance (W) |
|--|-----------|------------------------------|---------------------|
| 100 000 000 | 200 | Fusée Saturn V | 50 000 000 |
| 1 000 000 | 180 | | |
| 10 000 | 160 | Gros porteur quadriréacteurs | 50 000 |
| 100 | 140 | Grand orchestre | 10 |
| 1 | 120 | Marteau piqueur | 1 |
| 0.01 | 100 | Cri | 0.001 |
| 0.000 1 | 80 | | |
| 0.000 001 | 60 | Conversation | 20×10^{-6} |
| 0.000 000 01 | 40 | | |
| 0.000 000 000 1 | 20 | Chuchotement | 10^{-9} |
| 0.000 000 000 001 | 0 | | |
| Puissances acoustiques de sources courantes de bruit | | | |

Puissances acoustiques de sources courantes de bruit

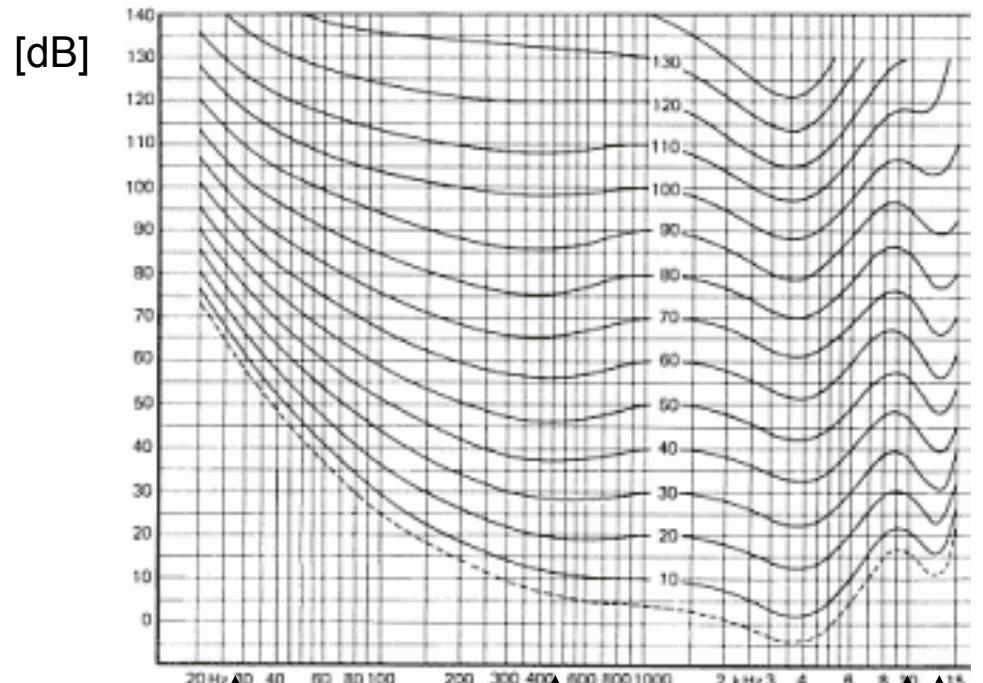


Courbes d'iso-niveaux physiologiques



[Hz]

Courbes d'iso-niveaux physiologiques



[Hz]

Pondération C

Pondération A

Sonomètre

